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Author: John Dee

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*** START OF THE PROJECT GUTENBERG EBOOK THE
MATHEMATICALL PRAEFACE TO ELEMENTS OF GEOMETRIE OF
EUCLID OF MEGARA ***

The variation in text sizes is as in the original.

In the printed book, all sidenotes were shown in the outer margin. For this e-text, they have been divided. Text sidenotes—including single numerals—are in the right margin; symbols are on the left, along with page numbers. The continuous quotation marks could not be reproduced, so they are shown as oversized open quotes “ and close quotes ” in the left margin.

The original book did not have numbered pages. Instead it labeled all recto (right-side) pages, grouped into six eight-page signatures. The signatures themselves have an unusual sequence: pointer (pointing finger); * (asterisk); a; b; c; A. The verso (left-side) pages were unmarked; they are identified here as ||. The [final page](#) was an unnumbered foldout, about twice the size of a normal page.

Unless otherwise noted, spelling and punctuation are unchanged. A few specific notes are given [at the end of the text](#), along with those passages of [Euclid](#) identified by number.

text linked below

[Title Page Text](#)

 The Translator to the Reader.

T(There) *Here is (gentle Reader) nothing (the word of God onely set apart) which so much beautifieth and adorneth the soule and minde of mā, as doth the knowledge of good artes and sciences: as the knowledge of naturall and morall Philosophie. The one setteth before our eyes, the creatures of God, both in the heauens aboue, and in the earth beneath: in which as in a glasse, we beholde the exceding maiestie and wisdom of God, in adorning and beautifying them as we see: in geuing vnto them such wonderfull and manifolde proprieties, and naturall workinges, and that so diuersly and in such varietie: farther in maintaining and conseruing them continually, whereby to praise and adore him, as by S. Paule we are taught. The other teacheth vs rules and preceptes of vertue, how, in common life amongst men, we ought to walke vprightly: what dueties pertaine to our selues, what pertaine to the gouernment or good order both of an housholde, and also of a citie or common wealth. The reading likewise of histories, conduceth not a litle, to the adorning of the soule & minde of man, a studie of all men cōmended: by it are seene and knowen the artes and doinges of infinite wise men gone before vs. In histories are contained infinite examples of heroicall vertues to be of vs followed, and horrible examples of vices to be of vs eschewed. Many other artes also there are which beautifie the minde of man: but of all other none do more garnishe & beautifie it, then those artes which are called Mathematicall. Unto the knowledge of which no man can attaine, without the perfecte knowledge and instruction of the principles, groundes, and Elementes of Geometrie. But perfectly to be instructed in them, requireth diligent studie and reading of olde auncient authors. Amongst which, none for a beginner is to be preferred before the*

most auncient Philosopher Euclide of Megara. For of all others he hath in a true methode and iuste order, gathered together whatsoeuer any before him had of these Elementes written: inuventing also and adding many thinges of his owne: wherby he hath in due forme accomplished the arte: first geuing definitions, principles, & groundes, wherof he deduceth his Propositions or conclusions, in such wonderfull wise, that that which goeth before, is of necessitie required to the proufe of that which followeth. So that without the diligent studie of Euclides Elementes, it is impossible to attaine vnto the perfecte knowledge of Geometrie, and consequently of any of the other Mathematicall sciences. Wherefore considering the want & lacke of such good authors hitherto in our Englishe tounge, lamenting also the negligence, and lacke of zeale to their countrey in those of our nation, to whom God hath geuen both knowledge, & also abilitie to translate into our tounge, and to publishe abroad such good authors, and bookes (the chiefe instrumentes of all learnings): seing moreouer that many good wittes both of gentlemen and of others of all degrees, much desirous and studious of these artes, and seeking for them as much as they can, sparing no paines, and yet frustrate of their intent, by no meanes attaining to that which they seeke: I haue for their sakes, with some charge & great trauaile, faithfully translated into our vulgare toũge, & set abroad in Print, this booke of Euclide. Whereunto I haue added easie and plaine declarations and examples by figures, of the definitions. In which booke also ye shall in due place finde manifolde additions, Scholies, Annotations, and Inuentions: which I haue gathered out of many of the most famous & chiefe Mathematiciẽs, both of old time, and in our age: as by diligent reading it in course, ye shall well perceauẽ. The fruite and gaine which I require for these my paines and trauaile, shall be nothing els, but onely that thou gentle reader, will gratefully accept the same: and that thou mayest thereby receaue some profite: and moreouer to excite and stirre vp others learned, to do the like, & to take paines in that behalfe. By meanes wherof, our Englishe tounge shall no lesse be enriched with good Authors, then are other straunge tounes: as the Dutch,

French, Italian, and Spanishe: in which are red all good authors in a maner, found amongst the Grekes or Latines. Which is the chieftest cause, that amongst thẽ do florishe so many cunning and skilfull men, in the inuentions of straunge and wonderfull thinges, as in these our daies we see there do. Which fruite and gaine if I attaine vnto, it shall encourage me hereafter, in such like sort to translate, and set abroad some other good authors, both pertaining to religion (as partly I haue already done) and also pertaining to the Mathematicall Artes. Thus gentle reader farewell.

(?;)



TO THE VNFAINED LOVERS

of truthe, and constant Studentes of Noble
Sciences, IOHN DEE of *London*, hartily
wisheth grace from heauen, and most prosperous
successe in all their honest attemptes and
exercises.

D(Divine) Iuine *Plato*, the great Master of many worthy Philosophers, and the constant auoucher, and pithy perswader of *Vnum*, *Bonum*, and *Ens*: in his Schole and Academie, sundry times (besides his ordinary Scholers) was visited of a certaine kinde of men, allured by the noble fame of *Plato*, and the great commendation of hys profound and profitable doctrine. But when such Hearers, after long harkening to him, perceaued, that the drift of his discourses issued out, to conclude, this *Vnum*, *Bonum*, and *Ens*, to be Spirituall, Infinite, Æternall, Omnipotent, &c. Nothyng beyng alledged or expressed, How, worldly goods: how, worldly dignitie: how, health, Strẽgth or lustines of body: nor yet the meanes, how a merueilous sensible and bodyly blysse and felicitie

hereafter, might be atteyned: Straightway, the fantasies of those hearers, were damp't: their opinion of *Plato*, was clene chaunged: yea his doctrine was by them despised: and his schole, no more of them visited. Which thing, his Scholer, *Aristotle*, narrowly cōsidering, founde the cause therof, to be, "For that they had no forwarnyng and information, in generall, whereto his doctrine tended. For, so, might they haue had occasion, either to haue forborne his schole hauntyng: (if they, then, had misliked his Scope and purpose) or constantly to haue continued therin: to their full satisfaction: if such his finall scope & intent, had ben to their desire. Wherefore, *Aristotle*, euer, after that, vsed in brief, to forewarne his owne Scholers and hearers, "both of what matter, and also to what ende, he tooke in hand to speake, or teach." While I consider the diuerse trades of these two excellent Philosophers (and am most sure, both, that *Plato* right well, otherwise could teach: and that *Aristotle* mought boldely, with his hearers, haue dealt in like sorte as *Plato* did) I am in no little pang of perplexitie: Bycause, that, which I mislike, is most easy for me to performe (and to haue *Plato* for my exāple.) And that, which I know to be most commendable: and (in this first bringyng, into common handling, the *Artes Mathematicall*) to be most necessary: is full of great difficultie and sundry daungers. Yet, neither do I think it mete, for so straunge matter (as now is ment to be published) and to so straunge an audience, to be bluntly, at first, put forth, without a peculiar Preface: Nor (Imitatyng *Aristotle*) well can I hope, that accordyng to the amplexes and dignitie of the *State Mathematicall*, I am able, either playnly to prescribe the materiall boundes: or precisely to expresse the chief purposes, and most wonderfull applications therof. And though I am sure, that such as did shrink from *Plato* his schole, after they had perceiued his finall conclusion, would in these thinges haue ben his most diligent hearers (so infinitely mought their desires, in fine and at length, by our *Artes Mathematicall* be satisfied) yet, by this my Præface & forewarnyng, Aswell all such, may (to their great behofe) the

soner, hither be allured: as also the *Pythagoricall*, and *Platonickall* perfect scholer, and the constant profound Philosopher, with more ease and spede, may (like the Bee,) gather, hereby, both wax and hony.

Wherefore, seyng I finde great occasion (for the causes alleged, and farder, in respect of my *Art Mathematicke generall*) to vs^e a certaine forewarnyng and Præface, whose content shalbe, *The intent of this Preface* most plesaunt, and frutefull *Mathematicall Tree*, with his chief armes and second (grifted) braunches: Both, what euery one is, and also, what commodity, in generall, is to be looked for, aswell of griff as stocke: And forasmuch as this enterprise is so great, that, to this our tyme, it neuer was (to my knowledge) by any achieued: And also it is most hard, in these our drery dayes, to such rare and straunge Artes, to wyn due and common credit[?]

Neuertheles, if, for my sincere endeuour to satisfie your honest expectation, you will but lend me your thākefull mynde a while: and, to such matter as, for this time, my penne (with spede) is hable to deliuer, apply your eye or eare attentifely: perchaunce, at once, and for the first salutying, this Preface you will finde a lesson long enough. And either you will, for a second (by this) be made much the apter: or shortly become, well hable your selues, of the lyons claw, to coniecture his royall symmetrie, and farder propertie. Now then, gentle, my frendes, and countrey men, Turne your eyes, and bend your myndes to that doctrine, which for our present purpose, my simple talent is hable to yeld you.

All thinges which are, & haue beyng, are found vnder a triple diuersitie generall. For, either, they are demed Supernaturall, Naturall, or, of a third being. Thinges Supernaturall, are immateriall, simple, indiuisible, incorruptible, & vnchangeable. Things Naturall, are materiall, compounded, diuisible, corruptible, and chaungeable. Thinges Supernaturall, are, of the minde onely, comprehended: Things Naturall, of the sense exterior, ar hable to be perceiued. In thinges Naturall, probabilitie and coniecture hath place: But in things Supernaturall, chief demōstration, & most sure

Science is to be had. By which properties & comparasons of these two, more easily may be described, the state, condition, nature and property of those thinges, which, we before termed of a third being: which, by a peculier name also, are called *Thynges Mathematicall*. For, these, beyng (in a maner) middle, betwene thinges supernaturall and naturall: are not so absolute and excellent, as thinges supernatural: Nor yet so base and grosse, as things naturall: But are thinges immateriall: and neuerthelesse, by materiall things hable somewhat to be signified. And though their particular Images, by Art, are aggregable and diuisible: yet the generall *Formes*, notwithstanding, are constant, vnchaungeable, vntrāsformable, and incorruptible. Neither of the sense, can they, at any tyme, be perceiued or iudged. Nor yet, for all that, in the royall mynde of man, first conceiued. But, surmountyng the imperfectiō of coniecture, weenyng and opinion: and commyng short of high intellectuall cōceptiō, are the Mercurial fruite of *Dianæticall* discourse, in perfect imagination subsistyg. A meruaylous newtralitie haue these thinges *Mathematicall*, and also a straunge participatiō betwene thinges supernaturall, immortall, intellectual, simple and indiuisible: and thynges naturall, mortall, sensible, compounded and diuisible. Probabilitie and sensible prose, may well serue in thinges naturall: and is commendable: In Mathematicall reasoninges, a probable Argument, is nothyng regarded: nor yet the testimony of sense, any whit credited: But onely a perfect demonstration, of truthe certaine, necessary, and inuincible: vniuersally and necessarily concluded: is allowed as sufficient for an Argument exactly and purely Mathematicall.

Of *Mathematicall* thinges, are two principall kindes: namely, *Number*, and *Magnitud*~~Number~~^{Number}, we define, to be, a certayne Mathematicall Sūme, of *Vnits*. *Note the worde, Vnit, to expresse the Greke Monas, & not Vnitie: as we haue all, commensurable, and incommensurable.* And, an *Vnit*, is that thing Mathematicall, Indiuisible, by participation of some likenes of whose property, any thing, which is in deede, or is counted One,

may reasonably be called One. We account an *Vnit*, a thing *Mathematicall*, though it be no Number, and also indiuisable: because, of it, materially, Number doth consist: which, principally, is a thing *Mathematicall*. ~~Magnitude is a thing~~ *Mathematicall*, by participation of some likenes of whose nature, any thing is iudged long, broade, or thicke. "A thicke *Magnitude* we call a *Solide*, or a *Body*. What *Magnitude* so euer, is Solide or Thicke, is also broade, & long. A broade magnitude, we call a *Superficies* or a *Plaine*. Euery playne magnitude, hath also length. A long magnitude, we terme a *Line*. A *Line* is neither thicke nor broade, but onely long: Euery certayne *Line*, hath two ends, ~~the ends of a line~~, are *Pointes* called. A *Point*, is a thing *Mathematicall*, indiuisable, which may haue a certayne determined situation." If a Poynt moue from a determined situation, the way wherein it moued, is also a *Line*: mathematically produced, whereupon, of the auncient *Mathematicians*, is called the race or course of a *Point*. A Poynt we define, by the name of a thing *Mathematicall*: though it be no *Magnitude*, and indiuisable: because it is the propre ende, and bound of a *Line*: which is a true *Magnitude*. And *Magnitude*, we may define to be that thing *Mathematicall*, which is diuisible for euer, in partes diuisible, long, broade or thicke. Therefore though a Poynt be no *Magnitude*, yet *Terminatiuely*, we reckon it a thing *Mathematicall* (as I sayd) by reason it is properly the end, and bound of a line. Neither *Number*, nor *Magnitude*, haue any Materialitie. First, we will consider of *Number*, and of the Science *Mathematicall*, to it appropriate, called *Arithmetike*: and afterward of *Magnitude*, and his Science, called *Geometrie*. But that name contenteth me not: whereof a word or two hereafter shall be sayd. How Immateriall and free from all matter, *Number* is, who doth not perceauē? yea, who doth not wonderfully wōder at it? For, neither pure *Element*, nor *Aristoteles*, *Quinta Essentia*, is hable to serue for Number, as his propre matter. Nor yet the puritie and simplenes of Substance Spirituall or Angelicall, will be found propre enough thereto. And therefore the great & godly

Philosopher *Anitius Boetius*, sayd: *Omnia quæcunq^{ue} a primæua rerum natura constructa sunt, Numerorum videntur ratione formata. Hoc enim fuit principale in animo Conditoris Exemplar.* That is: *All thinges (which from the very first originall being of thinges, haue bene framed and made) do appeare to be Formed by the reason of Numbers. For this was the principall example or patterne in the minde of the Creator.* O comfortable allurement, O rauishing perswasion, to deale with a Science, whose Subiect, is so Auncient, so pure, so excellent, so surmounting all creatures, so vsed of the Almighty and incomprehensible wisdom of the Creator, in the distinct creation of all creatures: in all their distinct partes, properties, natures, and vertues, by order, and most absolute number, brought, from *Nothing*, to the *Formalitie* of their being and state. By *Numbers* propertie therefore, of vs, by all possible meanes, (to the perfection of the Science) learned, we may both winde and draw our selues into the inward and deepe search and vew, of all creatures distinct vertues, natures, properties, and *Formes*: And also, farder, arise, clime, ascend, and mount vp (with Speculatiue winges) in spirit, to behold in the Glas of Creation, the *Forme of Formes*, the *Exemplar Number* of all thinges *Numerable*: both visible and inuisible, mortall and immortall, Corporall and Spirituall. Part of this profound and diuine Science, had *Ioachim* the Prophetesier atteyned vnto: by *Numbers Formall, Naturall, and Rationall*, forseyng, concludyng, and forshewyng great particular euent, long before their comming. His bookes yet remainyng, hereof, are good profe: And the noble Earle of *Mirandula*, (besides that,) a sufficient witnesse: that *Ioachim, in his prophetesies, proceeded by no other way, then by Numbers Formall.* And this Earle hym selfe, in *Romescet vpon 100.488* conclusions, in all kinde of Sciences, openly to be disputed of: and among the rest, in his *Conclusions Mathematicall*, (in the eleuenth Conclusion) hath in Latin, this English sentence. *By Numbers, a way is had, to the searchyng out, and vnderstandyng of euery thyng, hable to be knowen. For the verifying of which Conclusion, I promise to aunswere to the 74.*

Questions, vnder written, by the way of Numbers. Which Cōclusions, I omit here to rehearse: aswell auoidyng superfluous prolixitie: as, bycause *Ioannes Picus, workes*, are commonly had. But, in any case, I would wish that those Conclusions were red diligently, and perceiued of such, as are earnest Obseruers and Considerers of the constant law of nūbers: which is planted in thyngs Naturall and Supernaturall: and is prescribed to all Creatures, inuiolably to be kept. For, so, besides many other thinges, in those Conclusions to be marked, it would apeare, how sincerely, & within my boundes, I disclose the wonderfull mysteries, by numbers, to be atteyned vnto.

Of my former wordes, easy it is to be gathered, that *Number* hath a treble state: One, in the Creator: an other in euery Creature (in respect of his complete constitution:) and the third, in Spirituall and Angelicall Myndes, and in the Soule of mā. In the first and third state, *Number*, is termed *Number Numbryng*. But in all Creatures, otherwise, *Number*, is termed *Nūber Numbred*. And in our Soule, Nūber beareth such a swaye, and hath such an affinitie therwith: that some of the old *Philosophers* taught, *Mans Soule, to be a Number mouyng it selfe*. And in dede, in vs, though it be a very Accident: yet such an Accident it is, that before all Creatures it had perfect beyng, in the Creator, Sempiternally. *Number Numbryng* therefore, is the discretion discerning, and distincting of thinges. But in God the Creator, This discretion, in the beginnyng, produced orderly and distinctly all thinges. For his *Numbryng*, then, was his Creatyng of all thinges. And his Continuall *Numbryng*, of all thinges, is the Conseruation of them in being: And, where and when he will lacke an *Vnit*: there and then, that particular thyng shalbe *Discreated*. Here I stay. But our Seuerallyng, distinctyng, and *Numbryng*, createth nothyng: but of Multitude considered, maketh certaine and distinct determination. And albeit these thynges be waighty and truthe of great importance, yet (by the infinite goodnes of the Almighty *Ternarie*,) Artificiall Methods and easy wayes are made, by which the zelous Philosopher, may wyn nere this Riuerish *Ida*, this Mountayne of

Contemplation: and more then Contemplation. And also, though *Number*, be a thyng so Immateriall, so diuine, and æternall: yet by degrees, by litle and litle, stretchyng forth, and applying some likenes of it, as first, to thinges Spirituall: and then, bryngyng it lower, to thynges sensibly perceiued: as of a momentanye sounde iterated: then to the least thynges that may be seen, numerable: And at length, (most grossely,) to a multitude of any corporall thynges seen, or felt: and so, of these grosse and sensible thynges, we are trayned to learne a certaine Image or likenes of numbers: and to vse Arte in them to our pleasure and proffit. So grosse is our conuersation, and dull is our apprehension: while mortall Sense, in vs, ruleth the common wealth of our litle world. Hereby we say, Three Lyons, are three: or a *Ternarie*. Three Egles, are three, or a *Terna*~~Which~~* *Ternaries*, are eche, the *Vnion*, *knot*, and *Vniformitie*, of three discrete and distinct *Vnits*. That is, we may in eche *Ternarie*, thrise, seuerally pointe, and shew a part, *One*, *One*, and *One*. Where, in Numbryng, we say One, two, Three. But how farre, these visible Ones, do differre from our Indiuisable Vnits (in pure *Arithmetike*, principally considered) no man is ignorant. Yet from these grosse and materiall thynges, may we be led vpward, by degrees, so, informyng our rude Imagination, toward the cōceiuyng of *Numbers*, absolutely (:Not supposing, nor admixtyng any thyng created, Corporall or Spirituall, to support, conteyne, or represent those *Numbers* imagined:) that at length, we may be hable, to finde the number of our owne name, gloriously exemplified and registred in the booke of the *Trinitie* most blessed and æternall.

But farder vnderstand, that vulgar Practisers, haue Numbers, otherwise, in sundry Considerations: and extend their name farder, then to Numbers, whose least part is an *Vnit*. For the common Logist, Reckenmaster, or Arithmeticien, in hys vsing of Numbers: of an *Vnit*, imagineth lesse partes: and calleth them *Fractions*. As of an *Vnit*, he maketh an halfe, and thus noteth it, $\frac{1}{2}$. and so of other, (infinitely diuerse) partes of an *Vnit*. Yea and farder, hath, *Fractions of Fractions*. &c. And, forasmuch, as, *Addition*,

Substraction, Multiplication, Diuision and Extraction of Rotes, are the chief, and sufficient partes of *Arithmetike* which is the Science that demonstrateth the properties, of Numbers, and all operatiōs, in numbers to be performed. ~~How often, Note~~ Therefore, these fiue sundry sortes of Operations, do, for the most part, of their execution, differre from the fiue operations of like generall property and name, in our Whole numbers practisable, So often, (for a more distinct doctrine) we, vulgarly account and name it, an other kynde of *Arithmetike*. And by this Consideration, doctrine, and working, in whole numbers onely: where, of an *Vnit*, is no lesse part to be allowed: is named (as it were) an *Arithmetike* by it selfe. And so of the *Arithmetike of Fractions*, the necessary, wonderfull and Secret doctrine of Proportion, and proportionalytie hath purchased vnto it selfe a peculier maner of handlyng and workyng: and so may seme an other forme of *Arithmetike*. the *Astronomers*, for spede and more commodious calculation, haue deuised a peculier maner of orderyng nũbers, about theyr circular motions, by Sexagenes, and Sexagesmes. By Signes, Degrees and Minutes &c. which commonly is called the *Arithmetike of Astronomical or Phisicall Fractions*. That, haue I briefly noted, by the name of *Arithmetike Circular*. Bycause it is also vsed in circles, not *Astronomicall*. &c. And Numbers farder, and hath framed them, to take vpon them, the shew of *Magnitudes* propertie: Which is *Incommensurabilitie* and *Irrationalitie*. (For in pure *Arithmetike*, an *Vnit*, is the common Measure of all Numbers.) And, here, Nũbers are become, as Lynes, Playnes and Solides: some tymes *Rationall*, some tymes *Irrationall*. And haue propre and peculier characters, (as $\sqrt[2]{}$. $\sqrt[3]{}$. and so of other. ^A Which is to signifie *Rote Square*, *Rote Cubik*: and so forth:) & propre and peculier fashions in the fiue principall partes: Wherefore the practiser, estemeth this, a diuerse *Arithmetike* from the other. Practise bryngeth in, here, diuerse compoundyng of Numbers: as some tyme, two, three, foure (or more) *Radicall* nũbers, diuersly knit, by signes, of More & Lesse: as thus $\sqrt[2]{12} + \sqrt[3]{15}$. Or thus $\sqrt[4]{19} + \sqrt[3]{12} - \sqrt[2]{2}$. &c. And some tyme with whole

numbers, or fractions of whole Number, amōg them: as $20 + \sqrt[2]{24}$.
 $\sqrt[3]{16} + 33 - \sqrt[2]{10}$. $\sqrt[4]{44} + 12\frac{1}{4} + \sqrt[3]{9}$. And so, infinitely, may hap
 the varietie. After this: Both the one and the other hath fractions
 incident: and so is this *Arithmetike* greatly enlarged, by diuerse
 exhibityng and vse of Compositions and mixtynges. Consider how,
 I (beyng desirous to deliuer the student from error and Cauillation)
 do giue to this *Practise*, the name of the *Arithmetike of Radicall*
numbers: Not, of *Irrationall* or *Surd Numbers*: which other while,
 are *Rationall*: though they haue the Signe of a Rote before them,
 which, *Arithmetike* of whole Numbers most vsuall, would say they
 had no such Roote: and so account them *Surd Numbers*: which,
 generally spokē, is vntrue: as *Euclides* tenth booke may teach you.
 Therfore to call them, generally, *Radicall Numbers*, (by reason of
 the signe $\sqrt{}$. prefixed,) is a sure way: and a sufficient generall
 distinction from all other ordryng and vsing of Numbers: And yet
 (beside all this) Consider: the infinite desire of knowledge, and
 incredible power of mans Search and Capacitye: how, they, ioyntly
 haue waded farder (by mixtyng of speculation and practise) and
 haue found out, and atteyned to the very chief perfection (almost)
 of *Numbers* Practicall vse. Which thing, is well to be perceiued in
 that great Arithmeticall Arte of *Æquation*: commonly called the
Rule of Coss. or *Algebra*. The Latines termed it, *Regulam Rei &*
Census, that is, the *Rule of the thyng and his value*. With an apt
 name: comprehendynge the first and last pointes of the worke. And
 the vulgar names, both in Italian, Frenche and Spanish, depend (in
 namyng it,) vpon the signification of the Latin word, *Res: A thing*:
 vnleast they vse the name of *Algebra*. And therin (commonly) is a
 dubble error. The one, of them, which thinke it to be of *Geber* his
 inuentynge: the other of such as call it *Algebra*. For, first, though
Geber for his great skill in Numbers, Geometry, Astronomy, and
 other maruailous Artes, mought haue semed hable to haue first
 deuised the sayd Rule: and also the name carryeth with it a very
 nere likenes of *Geber* his name: yet true it is, that a *Greke*
 Philosopher and Mathematicien, named *Diophantus*, before *Geber*
 his tyme, wrote 13. bookes therof (of which, six are yet extant: and

I had them to *vse, of the famous Mathematicien, and my great frende, *Petrus Mont aureus* :) And secondly, the very name, is *Algiebar*, and not *Algebra*: as by the Arabien *Auicen*, may be proued: who hath these precise wordes in Latine, by *Andreas Alpagus* (most perfect in the Arabik tung) so translated. *Scientia faciendi Algiebar & Almachabel. i. Scientia inueniendi numerum ignotum, per additionem Numeri, & diuisionem & æquationem.* Which is to say: *The Science of workyng Algiebar and Almachabel*, that is, the *Science of findyng an vnknown number, by Addyng of a Number, & Diuision & æquation.* Here haue you the name: and also the principall partes of the Rule, touched. To name it, *The rule, or Art of Æquation*, doth signifie the middle part and the State of the Rule. This Rule, hath his peculier Characteristicall partes of *Arithmetike*, to it appertayning, do differre from the other *Arithmetically operations*. This *Arithmetike*, hath *Nũbers* Simple, Cõpound, Mixt: and Fractions, accordingly. This Rule, and *Arithmetike of Algiebar*, is so profound, so generall and so (in maner) conteyneth the whole power of Numbers Application practicall: that mans witt, can deale with nothyng, more proffitable about numbers: nor match, with a thyng, more mete for the diuine force of the Soule, (in humane Studies, affaires, or exercises) to be tryed in. Perchaunce you looked for, (long ere now,) to haue had some particular profe, or euident testimony of the vse, proffit and Commodity of *Arithmetike* vulgar, in the Common lyfe and trade of men. Therto, then, I will now frame my selfe: But herein great care I haue, least length of sundry profes, might make you deme, that either I did misdoute your zelous mynde to vertues schole: or els mistrust your hable witts, by some, to gesse much more. A profe then, foure, fiue, or six, such, will I bryng, as any reasonable man, therewith may be persuaded, to loue & honor, yea learne and exercise the excellent Science of *Arithmetike*.

And first: who, nerer at hand, can be a better witsse of the frute receiued by *Arithmetike*, then all kynde of Marchants? Though not all, alike, either nede it, or vse it. How could they forbear the vse

and helpe of the Rule, called the Golden Rule? Simple and Compound: both forward and backward? How might they misse *Arithmetically* helpe in the Rules of Fellowship: either without tyme, or with tyme? and betwene the Marchant & his Factor? The Rules of Bartering in wares onely: or part in wares, and part in money, would they gladly want? Our Marchant venturers, and Trauaylers ouer Sea, how could they order their doynge iustly and without losse, vnleast certaine and generall Rules for Exchaunge of money, and Rechaunge, were, for their vse, deuised? The Rule of Alligation, in how sundry cases, doth it conclude for them, such precise verities, as neither by naturall witt, nor other experience, they, were hable, els, to know? And (with the Marchant then to make an end) how ample & wonderfull is the Rule of False positions? especially as it is now, by two excellent Mathematiciens (of my familier acquayntance in their life time) enlarged? I meane *Gemma Frisius*, and *Simon Iacob*. Who can either in brief conclude, the generall and Capitall Rules? or who can Imagine the Myriades of sundry Cases, and particular examples, in Act and earnest, continually wrought, tried and concluded by the forenamed Rules, onely? How sundry other *Arithmetically practises*, are commonly in Marchantes handes, and knowledge: They them selues, can, at large, testifie.

The Mintmaster, and Goldsmith, in their Mixture of Metals, either of diuerse kindes, or diuerse values: how are they, or may they, exactly be directed, and meruailously pleased, if *Arithmetike* be their guide? And the honorable Phisiciāns, will gladly confesse them selues, much beholding to the Science of *Arithmetike*, and that sundry wayes: But chiefly in their Art of Graduation, and compoude Medicines. And though *Galenus*, *Auerrois*, *Arnoldus*, *Lullus*, and other haue published their positions, aswell in the quantities of the Degrees aboue Temperament, as in the Rules, concluding the new *Forme* resulting: yet a more precise, commodious, and easy *Method*, is extant: by a Countreyman of our 200th yeares ago) inuented. And forasmuch as I am vncertaine, who hath the same: or when that litle Latin treatise, (as the Author

writ it,) shall come to be Printed: (Both to declare the desire I haue to pleasure my Countrey, wherein I may: and also, for very good profe of Numbers vse, in this most subtile and frutefull, Philosophicall Conclusion,) I entend in the meane while, most briefly, and with my farder helpe, to communicate the pith therof vnto you.

First describe a circle: whose diameter let be an inch. Diuide the Circumference into foure equall partes. Frõ the Center, by those 4. sections, extend 4. right lines: eche of 4. inches and a halfe long: or of as many as you liste, aboue 4. without the circumference of the circle: So that they shall be of 4. inches long (at the least) without the Circle. Make good euident markes, at euery inches end. If you list, you may subdiuide the inches againe into 10. or 12. smaller partes, equall. At the endes of the lines, write the names of the 4. principall elementall Qualities. *Hote* and *Colde*, one against the other. And likewise *Moyst* and *Dry*, one against the other. And in the Circle write *Temperate*. Which *Temperature* hath a good Latitude: as appeareth by the Complexion of man. And therefore we haue allowed vnto it, the foresayd Circle: and not a point Mathematicall or Physicall. B

diagram: see end of text for alternative

** Take some part of Lullus counsayle in his booke de Q. Essentia.*

Now, when you haue two thinges Miscible, whose degrees are * truely knowen: Of necessitie, either they are of one Quantitie and waight, or of diuerse. If they be of one Quantitie and waight: whether their formes, be Contrary Qualities, or of one kinde (but of diuerse intentions and degrees) or a *Temperate*, and a Contrary, *The forme resulting of their Mixture, is in the Middle betwene the degrees of the formes mixt.* As for example, let *A*, be *Moist* in the first degree: and *B*, *Dry* in the third degree. Adde 1. and 3. that maketh 4: the halfe or middle of 4. is 2. This 2. is the middle, equally distant from *A* and *B* (for *Temperamentum* is counted none.

And for it, you must put a Ciphre, if at any time, it be in mixture). Counting then from *B*, 2. degrees, toward *A*: you finde it to be *Dry* in the first degree: So is the *Forme resulting* of the Mixture of *A*, and *B*, in our example. I will geue you an other example. Suppose, you haue two thinges, as *C*, and *D*: and of *C*, the Heate to be in the 4. degree: and of *D*, the Colde, to be remisse, euen vnto the *Temperament*. Now, for *C*, you take 4: and for *D*, you take a Ciphre: which, added vnto 4, yeldeth onely 4. The middle, or halfe, whereof, is 2. Wherefore the *Forme resulting* of *C*, and *D*, is Hote in the second degree: for, 2. degrees, accounted from *C*, toward *D*, ende iuste in the 2. degree of heate. Of the third maner, I will geue also an example: which let be these two Medicine whose Qualitie of heate is in the 4. degree exalted: as was *C*, in the example foregoing: and an other liquid Medicine I haue: whose Qualitie, is heate, in the first degree. Of eche of these, I mixt a like quantitie: Subtract here, the lesse frō the more: and the residue diuide into two equall partes: whereof, the one part, either added to the lesse, or subtracted from the higher degree, doth produce the degree of the *Forme resulting*, by this mixture of *C*, and *E*. As, if from 4. ye abate 1. there resteth 3. the halfe of 3. is $1\frac{1}{2}$: Adde to 1. this $1\frac{1}{2}$: you haue $2\frac{1}{2}$. Or subtract from 4. this $1\frac{1}{2}$: you haue likewise $2\frac{1}{2}$ remayning. Which declareth, the *Forme resulting*, to be *Heate*, in the middle of the third degree.

Be Sixthe Rule
 The *Effects* of two thinges Commixt, be diuerse, and the Intensions (of their *Formes Miscible*) be in diuerse degrees, and heigthes. (Whether those *Formes* be of one kinde, or of Contrary kindes, or of a Temperate and a Contrary, *What proportion is of the lesse quantitie to the greater, the same shall be of the difference, which is betwene the degree of the Forme resulting, and the degree of the greater quantitie of the thing miscible, to the difference, which is betwene the same degree of the Forme resulting, and the degree of the lesse quantitie.* As for example. Let two pound of Liquor be geuen, hote in the 4. degree: & one pound of Liquor be geuen, hote in the third degree. I would

gladly know the *Forme* resulting, in the Mixture of these two Liquors. Set downe your nũbers in order, thus. diagram: see end of text for alternative Now by the rule of Algiebar, haue I deuised a very easie, briefe, and generall maner of working in this case. Let vs first, suppose that *Middle Forme resulting*, to be $1X$: as that Rule teacheth. And because (by our Rule, here geuen) as the waight of 1. is to 2: So is the difference betwene 4. (the degree of the greater quantitie) and $1X$: to the difference betwene $1X$ and 3: (the degree of the thing, in lesse quãtitie. And with all, $1X$, being alwayes in a certaine middell, betwene the two heighthes or degrees). For the first difference, I set $4-1X$: and for the second, I set $1X-3$. And, now againe, I say, as 1. is to 2. so is $4-1X$ to $1X-3$. Wherefore, of these foure proportionall numbers, the first and the fourth Multiplied, one by the other, do make as much, as the second and the third Multiplied the one by the other. Let these Multiplications be made accordingly. And of the first and the fourth, we haue $1X-3$. and of the second & the third, $8-2X$. Wherefore, our Æquation is betwene $1X-3$: and $8-2X$. Which may be reduced, according to the Arte of Algiebar: as, here, adding 3. to eche part, geueth the Æquation, thus, $1X=11-2X$. And yet againe, contracting, or Reducing it: Adde to eche part, $2X$: Then haue you $3X$ æquall to 11: thus represented $3X=11$. Wherefore, diuiding 11. by 3: the Quotient is $3\frac{2}{3}$: the *Valew* of our $1X$, *Coss*, or *Thing*, first supposed. And that is the heigth, or Intension of the *Forme resulting*: which is, *Heate*, in two thirdes of the fourth degree: And here I set the shew of the worke in conclusion, thus. The proufe hereof is easie: by subtracting 3. from $3\frac{2}{3}$, diagram: see end of text for alternative resteth $\frac{2}{3}$. Subtracte the same heigth of the *Forme resulting*, (which is $3\frac{2}{3}$) frõ 4: then resteth $\frac{1}{3}$: You see, that $\frac{2}{3}$ is double to $\frac{1}{3}$: as 2.P. is double to 1.P. So should it be: by the rule here geuen. Note. As you added to eche part of the Æquation, 3: so if ye first added to eche part $2X$, it would stand, $3X-3=8$. And now adding to eche part 3: you haue (as afore) $3X=11$.

And though I, here, speake onely of two thyngs Miscible: and most commonly mo then three, foure, fiue or six, (&c.) are to be Mixed: (and in one Compound to be reduced: & the Forme resultyng of the same, to serue the turne) yet these Rules are sufficient: duely repeated and interpreted. ~~Interpreted~~ ^{Note} First, with any two: and then, with the Forme Resulting, and an other: & so forth: For, the last worke, concludeth the Forme resultyng of them all: I nede nothing to speake, of the Mixture (here supposed) what it is. Common Philosophie hath defined it, saying, *Mixtio est miscibilium, alteratorum, per minima coniunctorum, Vnio*. Euery word in the definition, is of great importance. I nede not also spend any time, to shew, how, the other manner of distributing of degrees, doth agree to these Rules. Neither nede I of the farder vse belonging to the Crosse of Graduation (before described) in this place declare, vnto such as are capable of that, which I haue all ready sayd. Neither yet with examples specifie the Manifold varieties, by the foresayd two generall Rules, to be ordered. The witty and Studious, here, haue sufficient: And they which are not hable to attaine to this, without liuely teaching, and more in particular: would haue larger discoursing, then is mete in this place to be dealt withall: And other (perchaunce) with a proude snuffe will disdaine this litle: and would be vnthankfull for much more. I, therefore conclude: and wish such as haue modest and earnest Philosophicall mindes, to laude God highly for this: and to Meruayle, that the profoundest and subtilest point, concerning *Mixture of Formes and Qualities Naturall*, is so Matcht and maryed with the most simple, easie, and short way of the noble Rule of *Algiebar*. Who can remaine, therefore vnpersuaded, to loue, alow, and honor the excellent Science of *Arithmetike*? For, here, you may perceiue that the litle finger of *Arithmetike*, is of more might and contriuing, then a hunderd thousand mens wittes, of the middle sorte, are hable to perfourme, or truely to conclude, with out helpe thereof.

Now will we farder, by the wise and valiant Capitaine, be certified, what helpe he hath, by the Rules of *Arithmetike*: in one of the

Artes to him appertaining: And of the Grekes named *ἡ Τεχνική*,
the Skill of Ordring Souldiers in Battell ray after the best maner to
all purposes. This Art so much dependeth vppon Numbers vse, and
the Mathematical, that *Ælianus* (the best writer therof,) in his
worke, to the *Emperour Hadrianus*, by his perfection, in the
Mathematicals, (beyng greater, then other before him had,)
thinketh his booke to passe all other the excellent workes, written
of that Art, vnto his dayes. For, of it, had written *Æneas: Cyneas*
of *Thessaly: Pyrrhus Epirota:* and *Alexander* his sonne: *Clearchus:*
Pausanias: Euangelus: Polybius, familier frende to *Scipio:*
Eupolemus: Iphicrates, Possidonius: and very many other worthy
Capitaines, Philosophers and Princes of Immortall fame and
memory: Whose fayrest floure of their garland (in this feat) was
Arithmetike: and a litle perceiuerance, in *Geometricall* Figures.
But in many other cases doth *Arithmetike* stand the Capitaine in
great stede. As in proportionyng of vittayles, for the Army, either
remaining at a stay: or suddenly to be encreased with a certaine
number of Souldiers: and for a certain tyme. Or by good Art to
diminish his company, to make the victuals, longer to serue the
remanent, & for a certaine determind tyme: if nede so require.
And so in sundry his other accountes, Reckeninges, Measurynges,
and proportionynges, the wise, expert, and Circumspect Capitaine
will affirme the Science of *Arithmetike*, to be one of his chief
Counsailors, directers and aiders. Which thing (by good meanes)
was euident to the Noble, the Couragious, the loyall, and Curteous
Iohn, late Earle of Warwicke. Who was a yong Gentleman,
thoroughly knowne to very few. Albeit his lusty valiantnes, force,
and Skill in Chiualrous feates and exercises: his humblenes, and
frendelynes to all men, were thinges, openly, of the world
perceiued. But what rotes (otherwise,) vertue had fastened in his
brest, what Rules of godly and honorable life he had framed to him
selfe: what vices, (in some then liuing) notable, he tooke great care
to eschew: what manly vertues, in other noble men, (florishing
before his eyes,) he Sythingly aspired after: what prowesses he
purposed and ment to achieue: with what feats and Artes, he began

to furnish and fraught him selfe, for the better seruice of his Kyng and Countrey, both in peace & warre. These (I say) his Heroicall Meditations, forecastinges and determinations, no twayne, (I thinke) beside my selfe, can so perfectly, and truely report. And therefore, in Conscience, I count it my part, for the honor, preferment, & procuring of vertue (thus, briefly) to haue put his Name, in the Register of *Fame Immortall*.

To our purpose. This *Iohn*, by one of his actes (besides many other: both in England and Fraunce, by me, in him noted.) did disclose his harty loue to vertuous Sciences: and his noble intent, to excell in Martiall prowesse: When he, with humble request, and instant Solliciting: got the best Rules (either in time past by Greke or Romaine, or in our time vsed: and new Stratagemes therein deuised) for ordning of all Companies, summes and Numbers of mē, (Many, or few) with one kinde of weapon, or mo, appointed: with Artillery, or without: on horsebacke, or on fote: to giue, or take onset: to seem many, being few: to seem few, being many. To marche in battaile or Iornay: with many such feates, to Foughten field, Skarmoush, or Ambushe appartaining: This noble Earle, dyed Anno. 1554. skarse of 24. yeares of age: hauing no issue by his wife: Daughter to the Duke of All these, liuely designementes (most curiously) to be in velame parchment described: with Notes & peculier markes, as the Arte requireth: and all these Rules, and descriptions Arithmetically, inclosed in a riche Case of Gold, he vsed to weare about his necke: as his Iuell most precious, and Counsaylour most trusty. Thus, *Arithmetike*, of him, was shryned in gold: Of *Numbers* frute, he had good hope. Now, Numbers therefore innumerable, in *Numbers* prayse, his shryne shall finde.

What nede I, (for farder profe to you) of the Scholemasters of Iustice, to require testimony: how nedefull, how frutefull, how skillfull a thing *Arithmetike* is? I meane, the Lawyers of all sortes. Vndoubtedly, the Ciuilians, can meruaylously declare: how, neither the Auncient Romaine lawes, without good knowledge of *Numbers art*, can be perceiued: Nor (Iustice in infinite Cases) without due proportion, (narrowly considered,) is hable to be

executed. How Iustly, & with great knowledge of Arte, did *Papinianus* institute a law of partition, and allowance, betwene man and wife after a diuorce? But how *Accursius*, *Baldus*, *Bartolus*, *Iason*, *Alexander*, and finally *Alciatus*, (being otherwise, notably well learned) do iumble, gesse, and erre, from the æquity, art and Intent of the lawmaker: *Arithmetike* can detect, and conuince: and clerely, make the truth to shine. Good *Bartolus*, tyred in the examining & proportioning of the matter: and with *Accursius* Glosse, much cumbred: burst out, and sayd: *Nulla est in toto libro, hac glossa difficilior: Cuius computationem nec Scholastici nec Doctores intelligunt. &c.* That is: *In the whole booke, there is no Glosse harder then this: Whose accoumpt or reckenyng, neither the Scholers, nor the Doctours vnderstand. &c.* What can they say of *Iulianus* law, *Si ita Scriptum. &c.* Of the Testators will iustly performing, betwene the wife, Sonne and daughter? How can they perceiue the æquitie of *Aphricanus*, *Arithmeticall* Reckening, where he treateth of *Lex Falcidia*? How can they deliuer him, from his Reprouers: and their maintainers: as *Ioannes*, *Accursius Hypolitus* and *Alciatus*? How Iustly and artificially, was *Africanus* reckening made? Proportionating to the Sommes bequeathed, the Contributions of eche part? Namely, for the hundred presently receiued, $17 \frac{1}{7}$. And for the hundred, receiued after ten monethes, $12 \frac{6}{7}$: which make the 30: which were to be cōtributed by the legataries to the heire. For, what proportion, 100 hath to 75: the same hath $17 \frac{1}{7}$ to $12 \frac{6}{7}$: Which is Sesquitertia: that is, as 4, to 3. which make 7. Wonderfull many places, in the Ciuile law, require an expert *Arithmeticien*, to vnderstand the deepe Iudgemēt, & Iust determinatiō of the Auncient Romaine Lawmakers. But much more expert ought he to be, who should be hable, to decide with æquitie, the infinite varietie of Cases, which do, or may happen, vnder euery one of those lawes and ordinances Ciuile. Hereby, easely, ye may now coniecture: that in the Canon law: and in the lawes of the Realme (which with vs, beare the chief Authoritie), Iustice and equity might be greatly preferred, and skilfully

executed, through due skill of Arithmetike, and proportions
 appertainyng. The worthy Philosophers, and prudent lawmakers
 (who haue written many bookes *De Republica*: How the best state
 of Common wealthes might be procured and mainteined,) haue
 very well determined of Iustice: (which, not onely, is the Base and
 foundation of Common weales: but also the totall perfection of all
 our workes, words, and thoughtes:) defining that *Iustice*, by
 which, to euery one, is rendred, that to him appertaineth. God
 challengeth this at our handes, to be honored as God: to be loued,
 as a father: to be feared as a Lord & master. Our neighbours
 proportiō, is also prescribed of the Almighty lawmaker: which is,
 to do to other, euen as we would be done vnto. These proportions,
 are in Iustice necessary: in duety, commendable: and of Common
 wealthes, the life, strength, stay and flourishing. *Aristotle* in his
Ethikes (to fatch the sede of Iustice, and light of direction, to vse
 and execute the same) was fayne to fly to the perfection, and
 power of Numbers: for proportions Arithmetically and
 Geometrically. *Plato* in his booke called *Epinomis* (which booke, is
 the Treasury of all his doctrine) where, his purpose is, to seke a
 Science, which, when a man had it, perfectly: he might seme, and
 so be, in dede, *Wise*. He, briefly, of other Sciences discoursing,
 findeth them, not hable to bring it to passe: But of the Science of
 Numbers, he sayth. *Illa, quæ numerum mortalium generi dedit, id
 profecto efficiet. Deum autem aliquem, magis quam fortunam, ad
 salutem nostram, hoc munus nobis arbitror contulisse. &c. Nam
 ipsum bonorum omnium Authorem, cur non maximi boni,
 Prudentiæ dico, causam arbitramur? That Science, verely,
 which hath taught mankynde number, shall be able to
 bryng it to passe. And, I thinke, a certaine God, rather then
 fortune, to haue giuen vs this gift, for our blisse. For, why
 should we not Iudge him, who is the Author of all good
 things, to be also the cause of the greatest good thyng,
 namely, *Wisedome*? There, at length, he proueth *Wisedome* to be
 atteyned, by good Skill of *Numbers*. With which great Testimony,*

and the manifold profes, and reasons, before expressed, you may be sufficiently and fully persuaded: of the perfect Science of *Arithmetike*, to make this account: To all Sciences, next to *Theologie*, it is most diuine, most pure, most ample and generall, most profounde, most subtile, most commodious and most necessary. Whose next Sister, is the Absolute Science of *Magnitudes*: of which (by the Direction and aide of him, whose *Magnitude* is Infinite, and of vs Incomprehensible) I now entend, so to write, that both with the *Multitude*, and also with the *Magnitude* of Meruaylous and frutefull verities, you (my frendes and Countreymen) may be stird vp, and awaked, to behold what certaine Artes and Sciences, (to our vnspeakable behofe) our heauenly father, hath for vs prepared, and reuealed, by sundry *Philosophers* and *Mathematiciens*.

Both, *Number* and *Magnitude*, haue a certaine Originall sede, (as it were) of an incredible property: and of man, neuer hable, Fully, to be declared. Of *Number*, an *Vnit*, and of *Magnitude*, a *Poynte*, doo seeme to be much like Originall causes: But the diuersitie neuerthesse, is great. We defined an *Vnit*, to be a thing Mathematicall Indiuisible: A Point, likewise, we sayd to be a Mathematicall thing Indiuisible. And farder, that a Point may haue a certaine determined Situation: that is, that we may assigne, and prescribe a Point, to be here, there, yonder. &c. Herein, (behold) our *Vnit* is free, and can abyde no bondage, or to be tyed to any place, or seat: diuisible or indiuisible. Agayne, by reason, a Point may haue a Situation limited to him: a certaine motion, therfore (to a place, and from a place) is to a Point incident and appertainyng. But an *Vnit*, can not be imagined to haue any motion. A Point, by his motion, produceth, Mathematically, a line: (as we sayd before) which is the first kinde of *Magnitudes*, and most simple: An *Vnit*, can not produce any number. A Line, though it be produced of a Point moued, yet, it doth not consist of pointes: Number, though it be not produced of an *Vnit*, yet doth it Consist of vnits, as a materiall cause. But formally, *Number* is the Vnion, and Vnitie of Vnits. Which vnytyng and knitting, is the workemanship of our

minde: which, of distinct and discrete Vnits, maketh a Number: by vniformitie, resulting of a certaine multitude of Vnits. And so, euery number, may haue his least part, giuen: namely, an Vnit: But not of a Magnitude, (no, not of a Lyne,) the least part can be giuē: by cause, infinitely, diuision therof, may be conceiued. All Magnitude, is either a Line, a Plaine, or a Solid. Which Line, Plaine, or Solid, of no Sense, can be perceiued, nor exactly by hād (any way) represented: nor of Nature produced: But, as (by degrees) Number did come to our perceiuerance: So, by visible formes, we are holpen to imagine, what our Line Mathematicall, is. What our Point, is. So precise, are our Magnitudes, that one Line is no broader then an other: for they haue no bredth: Nor our Plaines haue any thicknes. Nor yet our Bodies, any weight: be they neuer so large of dimensiō. Our Bodyes, we can haue Smaller, then either Arte or Nature can produce any: and Greater also, then all the world can comprehend. Our least Magnitudes, can be diuided into so many partes, as the greatest. As, a Line of an inch long, (with vs) may be diuided into as many partes, as may the diameter of the whole world, from East to West: or any way extended: What priuiledges, aboue all manual Arte, and Natures might, haue our two Sciences Mathematicall? to exhibite, and to deale with thinges of such power, liberty, simplicity, puritie, and perfection? And in them, so certainly, so orderly, so precisely to procede: as, excellent is that workemā Mechanicall Iudged, who nerest can approche to the representing of workes, Mathematically demonstrated. And our two Sciences, remaining pure, and absolute, in their proper termes, and in their owne Matter: to haue, and allowe, onely such Demonstrations, as are plaine, certaine, vniuersall, and of an æternall verity. This Science of Magnitude, his properties, conditions, and appertenances: commonly, now is, and from the beginnyng, hath of all Philosophers, ben called *Geometrie*. But, veryly, with a name to base and scant, for a Science of such dignitie and amplenes. And, perchaunce, that name, by cōmon and secret consent, of all wisemen, hitherto hath ben suffred to remayne: that it might carry with it a perpetuall memorye, of the first and notablest benefite, by that Science, to common people

shewed: Which was, when Boundes and meres of land and ground
 were lost, and confounded (as in *Egypt*, yearly, with the
 ouerflowyng of *Nilus*, the greatest and longest riuer in the world)
 or, that ground bequeathed, were to be assigned: or, ground sold,
 were to be layd out: or (when disorder preuailed) that Commōs
 were distributed into seueralties. For, where, vpon these & such
 like occasiōs, Some by ignorāce, some by negligēce, Some by
 fraude, and some by violence, did wrongfully limite, measure,
 encroach, or challenge (by pretence of iust content, and measure)
 those landes and groundes: great losse, disquietnes, murder, and
 warre did (full oft) ensue: Till, by Gods mercy, and mans Industrie,
 The perfect Science of Lines, Plaines, and Solides (like a diuine
 Iusticier,) gaue vnto euery man, his owne. The people then, by this
 art pleased, and greatly relieued, in their landes iust measuring:
 & other Philosophers, writing Rules for land measuring: betwene
 them both, thus, confirmed the name of *Geometria*, that is,
 (according to the very etimologie of the word) Land measuring.
 Wherin, the people knew no farder, of Magnitudes vse, but in
 Plaines: and the Philosophers, of thē, had no feet hearers, or
 Scholers: farder to disclose vnto, then of flat, plaine *Geometrie*.
 And though, these Philosophers, knew of farder vse, and best
 vnderstode the etymologie of the worde, yet this name *Geometria*,
 was of them applyed generally to all sortes of Magnitudes: vnleaste,
 otherwhile, of *Plato*, and *Pythagoras*: When they would precisely
 declare their owne doctrine. Then, was * ~~Platonetia~~ *Platonetia* with
 them, *Stadium quod circa planum versatur*. But, well you may
 perceiue by *Euclides Elementes*, that more ample is our Science,
 then to measure Plaines: and nothyng lesse therin is taught (of
 purpose) then how to measure Land. An other name, therefore, must
 nedes be had, for our Mathematicall Science of Magnitudes: which
 regardeth neither clod, nor turff: neither hill, nor dale: neither earth
 nor heauen: but is absolute *Megethologia*: not creping on ground,
 and dasseling the eye, with pole perche, rod or lyne: but liftynge the
 hart aboue the heauens, by inuisible lines, ~~and~~ mortall beames
 meteth with the reflexions, of the light incomprehensible: and so

procureth Ioye, and perfection vnspeakabl^e. Of which true vse of our *Megethica*, or *Megethologia*, *Diuine Plato* seemed to haue good taste, and iudgement: and (by the name of *Geometrie*) so noted it: and warned his Scholers therof: as, in hys seuenth *Dialog*, of the Common wealth, may euidently be sene. Where (in Latin) thus it is: right well translated: *Profecto, nobis hoc non negabunt, Quicunq^{ue} vel paululum quid Geometriæ gustârunt, quin hæc Scientia, contrà, omnino se habeat, quàm de ea loquuntur, qui in ipsa versantur.* In English, thus. *Verely (sayth Plato) whosoeuer haue, (but euen very litle) tasted of Geometrie, will not deny vnto vs, this: but that this Science, is of an other condicion, quite contrary to that, which they that are exercised in it, do speake of it.* And there it followeth, of our *Geometrie*, *Quòd quæritur cognoscendi illius gratia, quod semper est, non & eius quod oritur quandoq^{ue} & interit. Geometria, eius quod est semper, Cognitio est. Attollet igitur (ô Generose vir) ad Veritatem, animum: atq^{ue} ita, ad Philosophandum preparabit cogitationem, vt ad supera conuertamus: quæ, nunc, contra quàm decet, ad inferiora deijsimus. &c. Quàm maximè igitur præcipiendum est, vt qui præclarissimam hanc habitât Civitatem, nullo modo, Geometriam spernant. Nam & quæ præter ipsius propositum, quodam modo esse videntur, haud exigua sunt. &c.* It must nedes be confessed (saith *Plato*) *That [Geometrie] is learned, for the knowyng of that, which is euer: and not of that, which, in tyme, both is bred and is brought to an ende. &c. Geometrie is the knowledge of that which is euerlastyng. It will lift vp therfore (O Gentle Syr) our mynde to the Veritie: and by that meanes, it will prepare the Thought, to the Philosophicall loue of wisdome: that we may turne or conuert, toward heauenly thinges [both mynde and thought] which now, otherwise then becommeth vs, we cast down on base or inferior things. &c. Chiefly, therfore, Commaundement must be giuen, that such as do inhabit this most honorable*

Citie, by no meanes, despise Geometrie. For euen those thinges [done by it] which, in manner, seame to be, beside the purpose of Geometrie: are of no small importance. &c. And besides the manifold vses of *Geometrie*, in matters appertainyng to warre, he addeth more, of second vnpurposed frute, and commoditye, arrising by *Geometrie*: saying: *Scimus quin etiam, ad Disciplinas omnes facilius per discendas, interesse omnino, attigerit ne Geometriam aliquis, an non. &c. Hanc ergo Doctrinam, secundo loco discendam luuenibus statuamus.* That is. *But, also, we know, that for the more easy learnyng of all Artes, it importeth much, whether one haue any knowledge in Geometrie, or no. &c. Let vs therfore make an ordinance or decree, that this Science, of young men shall be learned in the second place.* This was *Diuine Plato* his Iudgement, both of the purposed, chief, and perfect vse of *Geometrie*: and of his second, dependyng, deriuatiue commodities. And for vs, Christen men, a thousand thousand mo occasions are, to haue nede of the helpe of* *I. D.*

* *Herein, I would gladly shake of, the earthly name of Geometricall* Contemplations: wherby, to trayne our Imaginations and Myndes, by litle and litle, to forsake and abandon, the grosse and corruptible Obiectes, of our vtward senses: and to apprehend, by sure doctrine demonstratiue, Things Mathematicall. And by them, readily to be holpen and conducted to conceiue, discourse, and conclude of things Intellectual, Spirituall, æternall, and such as concerne our Blisse euerlasting: which, otherwise (without Speciall priuiledge of Illumination, or Reuelation frõ heauen) No mortall mans wyt (naturally) is hable to reach vnto, or to Compasse. And, veryly, by my small Talent (from aboue) I am hable to proue and testifie, that the litterall Text, and order of our diuine Law, Oracles, and Mysteries, require more skill in Numbers, and Magnitudes: then (commonly) the expositors haue vttered: but rather onely (at the most) so warned: & shewed their own want therin. (To name any, is nedeles: and to note the places, is, here, no place: But if I be duely asked, my answeere is ready.)

And without the litterall, Grammaticall, Mathematicall or Naturall
 verities of such places, by good and certaine Arte, perceiued, no
 Spirituall sense (propre to those places, by Absolute *Theologie*)
 will thereon depend. And man, therefore, can doute, but toward the
 atteyning of knowledge incomparable, and Heauenly Wisedome:
 Mathematicall Speculations, both of Numbers and Magnitudes: are
 meanes, aydes, and guides: ready, certaine, and necessary. From
 henceforth, in this my Preface, will I frame my talke, to *Plato* his
 fugitiue Scholers: or, rather, to such, who well can, (and also wil,)
 vse their vtward senses, to the glory of God, the benefite of their
 Countrey, and their owne secret contentation, or honest
 preferment, on this earthly Scaffold. To them, I will orderly recite,
 describe & declare a great Number of Artes, from our two
 Mathematicall fountaines, deriued into the fieldes of *Nature*.
 Wherby, such Sedes, and Rotes, as lye depe hyd in the groūd of
Nature, are refreshed, quickened, and prouoked to grow, shote vp,
 floure, and giue frute, infinite, and incredible. And these Artes,
 shalbe such, as vpon Magnitudes properties do depende, more,
 then vpon Number. And by good reason we may call them Artes,
 and Artes Mathematicall Deriuatiue: for (at this tyme) I Define
 Arte, to be a Methodicall cōplete Doctrine, hauing
 abundancy of sufficient, and peculier matter to deale with,
 by the allowance of the Metaphisicall Philosopher: the
 knowledge whereof, to humaine state is necessarye. And
 that I account, *Art Mathematicall*. And *Art Mathematicall*
 deriuatiue, which by Mathematicall demonstratiue Method,
 in Nũbers, or Magnitudes, ordreth and confirmeth his
 doctrine, as much & as perfectly, as the matter subiect will
 admit. And for that, I entend to vse the name and propertie of a
~~Mechanicien~~ *Mechanicien*, rather, then (hitherto) it hath ben vsed, I thinke
 it good, (for distinction sake) to giue you also a brief description,
 what I meane therby. A Mechanicien, or a Mechanicall
 workman is he, whose skill is, without knowledge of
 Mathematicall demonstration, perfectly to worke and

finishe any sensible worke, by the Mathematicien principall or deriuatiue, demonstrated or demonstrable. Full well I know, that he which inuenteth, or maketh these demonstrations, is generally called *A speculatiue Mechanicien*: which differreth nothyng from a *Mechanicall Mathematicien*. So, in respect of diuerse actions, one man may haue the name of sundry artes: as, some tyme, of a Logicien, some tymes (in the same matter otherwise handled) of a Rethoricien. Of these trifles, I make, (as now, in respect of my Preface,) small account: to fyle thẽ for the fine handlyng of subtile curious disputers. In other places, they may commaunde me, to giue good reason: and yet, here, I will not be vnreasonable.

, from the puritie, absolutenes, and Immaterialitie of Principall *Geometrie*, is that kinde of *Geometrie* deriued, which vulgarly is counted *Geometrie*: and is the Arte of Measuring sensible magnitudes, their iust quãtities and contentes. *Geometrie* ~~cheth to~~ measure, either at hand: and the practiser, to be by the thing Measured: and so, by due applying of Cumpase, Rule, Squire, Yarde, Ell, Perch, Pole, Line, Gaging rod, (or such like instrument) to the Length, Plaine, or Solide*~~measured~~, either of the length, perimetry, or distance lineall: and this is called, *Mec*measured* of the content of any plaine Superficies: whether it be in ground Surueyed, Borde, or Glasse measured, or such like thing: which measuring, is named *Emb*measured*. 3. vnderstand the Soliditie, and content of any bodily thing: as of Tymber and Stone, or the content of Pits, Pondes, Wells, Vessels, small & great, of all fashions. Where, of Wine, Oyle, Beere, or Ale vessells, &c, the Measuring, commonly, hath a peculier name: and is called *Gaging*. And the generall name of these Solide measures, is *Steele*, ~~or, this~~ *vulgar Geometrie*, hath consideration to teach the practiser, how to measure things, with good distance betwene him and the thing measured: and to vnderstand ther*~~by~~, ~~how~~, ~~farre~~, a thing seene (on land or water) is from the measurer: and this may be called *Apon*, ~~or, how~~ *High or depe*, aboue or vnder the leuel of the measurers stãding, any thing is, which is sene on land or water,

called *Hypometrie* informeth the measurer, how Broad any thing is, which is in the measurers view: so it be on Land or Water, situated: and may be called *Platometrie*. Though I vse here to condition, the thing measured, to be on Land, or Water ~~Situated~~ ^{Situated} ~~Not~~ ^{Not} certaine, that the sundry heigthe of Cloudes, blasing Starres, and of the Mone, may (by these meanes) haue their distances from the earth: and, of the blasing Starres and Mone, the Soliditie (aswell as distances) to be measured: But because, neither these things are vulgarly taught: nor of a common practiser so ready to be executed: I, rather, let such measures be reckened incident to some of our other Artes, dealing with thinges on high, more purposely, then this vulgar Land measuring Geometrie doth: as in *Perspectiue* and *Astronomie*, &c.

OF these Feates (farther applied) is Sprong the Feate of *Geodesie*, or Land Measuring: more cunningly to measure & Suruey Land, Woods, and Waters, a farre of. More cunningly, I say: But God knoweth (hitherto) in these Realmes of England and Ireland (whether through ignorance or fraude, I can not tell, in euery part ~~how great Wrong~~ ^{how great Wrong} and iniurie hath (in my time) bene committed by vntrue measuring and surueying of Land or Woods, any way. And, this I am sure: that the Value of the difference, betwene the truth and such Surueyes, would haue bene hable to haue foūd (for euer) in eche of our two Vniuersities, an excellent Mathematicall Reader: to eche, allowing (yearly) a hundred Markes of lawfull money of this realme: which, in dede, would seme requisit, here, to be had (though by other wayes prouided for) as well, as, the famous Vniuersitie of Paris, hath two Mathematicall Readers: and eche, two hundreth French Crownes yearly, of the French Kinges magnificent liberalitie onely. Now, againe, to our purpose returning: Moreouer, of the former knowledge Geometricall, are growen the Skills of *Geographie*, *Chorographie*, *Hydrographie*, and *Stratarithmetrie*.

· **Geographie** teacheth wayes, by which, in sūdry formes, (as *Sphaerike*, *Plaine* or other), the Situation of Cities, Townes,

Villages, Fortes, Castells, Mountaines, Woods, Hauens, Riuers, Crekes, & such other things, vpō the outface of the earthly Globe (either in the whole, or in some principall mēber and portion therof cōtayned) may be described and designed, in cōmensurations Analogicall to Nature and veritie: and most aptly to our vew, may be represented[”]. Of this Arte how great pleasure, and how manifolde commodities do come vnto vs, daily and houely: of most men, is perceaued. While, some, to beautifie their Halls, Parlers, Chambers, Galeries, Studies, or Libraries with: other some, for thinges past, as battels fought, earthquakes, heauenly fyringes, & such occurentes, in histories mentioned: therby liuely, as it were, to vewe the place, the region adioyning, the distance from vs: and such other circumstances. Some other, presently to vewe the large dominion of the Turke: the wide Empire of the Moschouite: and the litle morsell of ground, where Christendome (by profession) is certainly knowen. Litle, I say, in respecte of the rest. &c. Some, either for their owne iorneyes directing into farre landes: or to vnderstand of other mens trauailes. To conclude, some, for one purpose: and some, for an other, liketh, loueth, getteth, and vseth, Mappes, Chartes, & Geographicall Globes. Of whose vse, to speake sufficiently, would require a booke peculier.

Chorographie seemeth to be an vnderling, and a twig, of *Geographie*: and yet neuerthelesse, is in practise manifolde, and in vse very ample[“]. This teacheth Analogically to describe a small portion or circuite of ground, with the contentes: not regarding what commensuration it hath to the whole, or any parcell, without it, contained. But in the territory or parcell of ground which it taketh in hand to make description of, it leaueth out (or vndescribed) no notable, or odde thing, aboue the ground visible. Yea and sometimes, of thinges vnder ground, geueth some peculier marke: or warning: as of Mettall mines, Cole pittes, Stone quarries. &c[”]. Thus, a Dukedome, a Shiere, a Lordship, or lesse, may be described distinctly. But marueilous pleasant, and

profitable it is, in the exhibiting to our eye, and commensuration, the plat of a Citie, Towne, Forte, or Pallace, in true Symmetry: not approaching to any of them: and out of Gunne shot. &c. Hereby, the *Architect* may furnishe him selfe, with store of what patterns he liketh: to his great instruction: euen in those thinges which outwardly are proportioned: either simply in them selues: or respectiue, to Hilles, Riuers, Hauens, and Woods adioyning. Some also, terme this particular description of places, *Topographie*.

· **Hydrographie**, deliuereth to our knowledge, on Globe or in Plaine, the perfect Analogicall description of the Ocean Sea coastes, through the whole world: or in the chiefe and principall partes thereof²²: with the Iles and chiefe particular places of daungers, conteyned within the boundes, and Sea coastes described: as, of Quicksandes, Bankes, Pittes, Rockes, Races, Countertides, Whorlepooles. &c. This, dealeth with the Element of the water chiefly: as *Geographie* did principally take the Element of the Earthes description (with his appertenances) to taske. And besides thys, *Hydrographie*, requireth a particular Register of certaine Landmarkes (where markes may be had) from the sea, well hable to be skried, in what point of the Seacumpase they appeare, and what apparent forme, Situation, and bignes they haue, in respecte of any daungerous place in the sea, or nere vnto it, assigned: And in all Coastes, what Mone, maketh full Sea: and what way, the Tides and Ebbes, come and go, the *Hydrographer* ought to recorde. The Soundinges likewise: and the Chanelles wayes: their number, and depthes ordinarily, at ebbe and flud, ought the *Hydrographer*, by obseruation and diligence of *Measuring*, to haue certainly knowen. And many other pointes, are belonging to perfecte *Hydrographie*, and for to make a *Rutter*, by: of which, I nede not here speake: as of the describing, in any place, vpon Globe or Plaine, the 32. pointes of the Compase, truely: (wherof, scarsly foure, in England, haue right knowledge: because, the lines therof, are no straight lines, nor Circles.) Of

making due proiection of a Sphere in plaine. Of the Variacion of the Compas, from true Northe: And such like matters (of great importance, all) I leaue to speake of, in this place: bycause, I may seame (al ready) to haue enlarged the boundes, and duety of an Hydrographer, much more, then any man (to this day) hath noted, or prescribed. Yet am I well hable to proue, all these thinges, to appertaine, and also to be proper to the Hydrographer. The chief vse and ende of this Art, is the Art of Nauigation: but it hath other diuerse vses: euen by them to be enioyed, that neuer lacke sight of land.

Stratarithmetrie, is the Skill, (appertainyng to the warre,) by which a man can set in figure, analogicall to any *Geometricall* figure appointed, any certaine number or summe of men: of such a figure capable: (by reason of the vsuall spaces betwene Souldiers allowed: and for that, of men, can be made no Fractions. Yet, neuertheles, he can order the giuen summe of men, for the greatest such figure, that of them, cã be ordred) and certifie, of the ouerplus: (if any be) and of the next certaine summe, which, with the ouerplus, will admit a figure exactly proportionall to the figure assigned. By which Skill, also, of any army or company of men: (the figure & sides of whose orderly standing, or array, is knowen) he is able to expresse the iust number of men, within that figure contained: or (orderly) able to be contained. And this *Figure*, and sides therof, he is hable to know: either beyng by, and at hand: or a farre of. Thus farre, stretcheth the description and property of *Stratarithmetrie*: sufficient for this tyme and place. *The*

difference betwene Stratarithmetrie and the Feate ~~“The difference between the Feate~~ *Tacticall, De aciebus instruendis.* bycause, there, is necessary the wisdom and foresight, to what purpose he so ordreth the men: and Skillfull hability, also, for any occasion, or purpose, to deuise and vse the aptest and most necessary order, array and figure of his Company and Summe of men.” By figure, I meane: as, either of a *Perfect Square, Triangle, Circle, Ouale, long square*, (of the Grekes it is called Eteromekes) *Rhombe, Rhomboid, Lunular,*

Ryng, Serpentine, and such other Geometricall figures: Which, in warres, haue ben, and are to be vsed: for commodiousnes, necessity, and auauntage &c. And no small skill ought he to haue, that should make true report, or nere the truth, of the numbers and Summes, of footemen or horsemen, in the Enemyes ordring. A farre of, to make an estimate, betwene nere termes of More and Lesse, is not a thyng very rife, among those that gladly would do it. *I. D.*

Frende,

*you will finde it hard, to performe my description of this Feate. But by Chorographie, you may helpe your selfe some what: where the Figures knowne (in Sides and Angles) are not Regular: And where, Resolution into Triangles can serue. &c. And yet you will finde it strange to deale thus generally with Arithmeticall figures: and, that for Battayle ray. Their contentes, differ so much from like Great pollicy may be vsed of the Capitaines, (at tymes fete, and in places conuenient) as to vse Figures, which make greatest shew, of so many as he hath: and vsing the aduauntage of the three kindes of vsuall spaces: (betwene footemen or horsemen) to take the largest: or when he would seme to haue few, (beyng many:) contrarywise, in Figure, and space. The Herald, Purseuant, Sergeant Royall, Capitaine, or who soeuer is carefull to come nere the truth herein, besides the Iudgement of his expert eye, his skill of Ordering *Tacticall*, the helpe of his Geometricall instrument: Ring, or Staffe Astronomicall: (commodiously framed for cariage and vse) He may wonderfully helpe him selfe, by perspectiue Glasses. In which, (I trust) our posterity will proue more skillfull and expert, and to greater purposes, then in these dayes, can (almost) be credited to be possible.*

Thus haue I lightly passed ouer the Artificiall Feates, chiefly dependyng vpon vulgar *Geometrie*: & commonly and generally reckened vnder the name of *Geometrie*. But there are other (very many) *Methodicall Artes*, which, declyning from the purity, simplicitie, and Immateriality, of our Principall Science of *Magnitudes*: do yet neuertheles vse the great ayde, direction, and Method of the sayd principall Science, and haue propre names, and distinct: both from the Science of *Geometrie*, (from which they are deriued) and one from the other. As *Perspectiue*, *Astronomie*, *Musike*, *Cosmographie*, *Astrologie*, *Statike*, *Anthropographie*, *Trochilike*, *Helicosophie*, *Pneumatithmie*, *Menadrie*, *Hypogeiodie*, *Hydragogie*, *Horometrie*, *Zographie*, *Architecture*, *Nauigation*, *Thaumaturgike* and *Archemastrie*. I thinke it necessary, orderly, of these to giue some peculier descriptions: and withall, to touch some of their commodious vses, and so to make this Preface, to be a little swete, pleasant Nosegaye for you: to comfort your Spirites, beyng almost out of courage, and in despayre, (through brutish brute) Weenyng that *Geometrie*, had but serued for buildyng of an house, or a curious bridge, or the roufe of Westminster hall, or some witty pretty deuise, or engyn, appropriate to a Carpenter, or a Ioyner &c. That the thing is farre otherwise, then the world, (commonly) to this day, hath demed, by worde and worke, good profe wilbe made.

Among these Artes, by good reason, **Perspectiue** ought to be had, ere of *Astronomicall Apparences*, perfect knowledge can be atteyned. And bycause of the prerogatiue of *Light*, beyng the first of *Gods Creatures*: and the eye, the light of our body, and his Sense most mighty, and his organ most Artificiall and *Geometricall*: At *Perspectiue*, we will begyn therfore. *Perspectiue*, is an Art Mathematicall, which demonstrateth the maner, and properties, of all Radiations Direct, Broken,

and Reflected. This Description, or Notation, is brief: but it reacheth so farre, as the world is wyde. It concerneth all Creatures, all Actions, and passions, by Emanation of beames perfourmed. Beames, or naturall lines, (here) I meane, not of light onely, or of colour (though they, to eye, giue shew, witnes, and profe, wherby to ground the Arte vpon) but also of other *Formes*, both *Substantiall*, and *Accidental*, the certaine and determined actiue Radiall emanations. By this Art (omitting to speake of the highest pointes) we may vse our eyes, and the light, with greater pleasure: and perfecter Iudgement: both of things, in light seen, & of other: which by like order of Lightes Radiations, worke and produce their effectes. We may be ashamed to be ignorant of the cause, why so sundry wayes our eye is deceiued, and abused: as, while the eye weeneth a roūd Globe or Sphere (beyng farre of) to be a flat and plaine Circle, and so likewise iudgeth a plaine Square, to be roūd: supposeth walles parallels, to approche, a farre of: rofe and floure parallels, the one to bend downward, the other to rise vppward, at a little distance from you. Againe, of thinges being in like swiftnes of mouing, to thinke the nerer, to moue faster: and the farder, much slower. Nay, of two thinges, wherof the one (incomparably) doth moue swifter then the other, to deme the slower to moue very swift, & the other to stand: what an error is this, of our eye? Of the Raynbow, both of his Colours, of the order of the colours, of the bignes of it, the place and heith of it, (&c) to know the causes demonstratiue, is it not pleasant, is it not necessary? of two or three Sonnes appearing: of Blasing Sterres: and such like thinges: by naturall causes, brought to passe, (and yet neuertheles, of farder matter, Significatiue) is it not commodious for man to know the very true cause, & occasion Naturall? Yea, rather, is it not, greatly, against the Souerainty of Mans nature, to be so ouershot and abused, with thinges (at hand) before his eyes? as with a Pecoockes tayle, and a Doues necke: or a whole ore, in water, holden, to seme broken. Thynges, farre of, to seeme nere: and nere, to seme farre of. Small thinges, to seme great: and great, to seme small. One man, to seme an Army. Or a

man to be curstly affrayed of his owne shaddow. Yea, so much, to feare, that, if you, being (alone) nere a certaine glasse, and proffer, with dagger or sword, to foyne at the glasse, you shall suddenly be moued to giue backe (in maner) by reason of an *A marueilous* ~~Glasse~~ *Glasse* in the ayre, betwene you & the glasse, with like hand, sword or dagger, & with like quicknes, foyning at your very eye, likewise as you do at the Glasse. Straunge, this is, to heare of: but more meruailous to behold, then these my wordes can signifie. And neuerthelesse by demonstration Opticall, the order and cause therof, is certified: euen so, as the effect is consequent. Yea, thus much more, dare I take vpon me, toward the satisfying of the noble courage, that longeth ardently for the wisdom of Causes Naturall: as to let him vnderstand, that, in London, he may with his owne eyes, haue profe of that, which I haue sayd herein.

A Gentleman, (which, for his good seruice, done to his Countrey, is famous and honored for skill in the Mathematicall Sciences, and Languages, is the Od man of this land. &c.) euen he, is hable: and (I am sure) will, very willingly, let the Glasse, and profe be sene: and so I (here) request him: for the encrease of wisdom, in the honorable: and for the stopping of the mouthes malicious: and repressing the arrogancy of the ignorant. Ye may easily gesse, what I meane. This Art of *Perspectiue*, is of that excellency, and may be led, to the certifying, and executing of such thinges, as no man would easily beleue: without Actuell profe perceiued.

I speake nothing of *Naturall Philosophie*, which, without *Perspectiue*, can not be fully vnderstanded, nor perfectly attained vnto. Nor, of *Astronomie*: which, without *Perspectiue*, can not well be grounded: Nor *Astrologie*, naturally Verified, and auouched.

That part hereof, which dealeth with Glasses (which name, Glasse, is a generall name, in this Arte, for any thing, from which, a Beame reboundeth) is called *Catoptrike*: and hath so many vses, both merueilous, and profitable: that, both, it would hold me to long, to note therein the principall conclusions, all ready knowne: And also (perchaunce) some thinges, might lacke due credite with you: And I, therby, to leese my labor: and you, to slip into light

Iudgement. Before you haue learned sufficiently the powre of Nature and Arte.

Now, to procede: **Astronomie**, is an Arte Mathematicall, which demonstrateth the distance, magnitudes, and all naturall motions, apparences, and passions propre to the Planets and fixed Sterres: for any time past, present and to come: in respect of a certaine Horizon, or without respect of any Horizon. By this Arte we are certified of the distance of the Starry Skye, and of eche *Planete* from the Centre of the Earth: and of the greatnes of any Fixed starre sene, or *Planete*, in respect of the Earthes greatnes. As, we are sure (by this Arte) that the Solidity, Massines and Body of the *Sonne*, conteineth the quantitie of the whole Earth and Sea, a hundred thre score and two times, lesse by $\frac{1}{8}$ one eight parte of the earth. But the Body of the whole earthly globe and Sea, is bigger then the body of the *Mone*, three and forty times lesse by $\frac{1}{8}$ of the *Mone*. Wherefore the *Sonne* is bigger then the *Mone*, 7000 times, lesse, by $59 \frac{39}{64}$ that is, precisely $6940 \frac{25}{64}$ bigger then the *Mone*. And yet the vnskillfull man, would iudge them a like bigge. Wherefore, of Necessity, the one is much farder from vs, then the other. The *Sonne*, when he is fardest from the earth (which, now, in our age, is, when he is in the 8. degree, of Cancer) is, 1179 Semidiameters of the Earth, distante. And the *Mone* when she is fardest from the earth, is 68 Semidiameters of the earth and $\frac{1}{3}$ The nerest, that the *Mone* commeth to the earth, is Semidiameters $52 \frac{1}{4}$ The distance of the Starry Skye is, frõ vs, in Semidiameters of the earth $20081 \frac{1}{2}$ Twenty thousand fourescore, one, and almost a halfe. Subtract from this, the *Mones* nerest distance, from the Earth: and therof remaineth Semidiameters of the earth $20029 \frac{1}{4}$ Twenty thousand nine and twenty and a ~~Quarter~~ ^{Quarter} is ~~the~~ ^{the} heavenly Palace, that the *Planetes* haue all their exercise in, and most meruailously perfourme the Commaũdement and Charge to them giuen by the omnipotent Maiestie of the king of kings. This is that, which in *Genesis* is called *Ha Rakia*. Consider it well. The Semidiameter of

the earth, cōteineth of our common miles 3436 $\frac{4}{11}$ three thousand, foure hundred thirty six and foure eleuenth partes of one myle: Such as the whole earth and Sea, round about, is 21600. One and twenty thousand six hundred of our myles. Allowyng for euery degree of the greatest circle, thre score myles. Now if you way well with your selfe but this litle parcell of frute *Astronomicall*, as concerning the bignesse, Distances of *Sonne*, *Mone*, *Sterry Sky*, and the huge massines of *Ha Rakia*, will you not finde your Consciencs moued, with the kingly Prophet, to sing the confession of Gods Glory, and say, *The Heauens declare the glory of God, and the Firmament* [*Ha Rakia*] *sheweth forth the workes of his handes*. And so forth, for those fiue first staues, of that kingly Psalme. Well, well, It is time for some to lay hold on wisdom, and to Iudge truly of thinges: and notso to expound the Holy word, all by Allegories: as to Neglect the wisdom, powre and Goodnes of God, in, and by his Creatures, and Creation to be seen and learned. By parables and Analogies of whose natures and properties, the course of the Holy Scripture, also, declareth to vs very many Mysteries. The whole Frame of Gods Creatures, (which is the whole world,) is to vs, a bright glasse: from which, by reflexion, reboundeth to our knowledge and perceiuerance, Beames, and Radiations: representing the Image of his Infinite goodnes, Omnipotēcy, and wisdom. And we therby, are taught and persuaded to Glorifie our Creator, as God: and be thankfull therfore. Could the Heathenistes finde these vses, of these most pure, beawtifull, and Mighty Corporall Creatures: and shall we, after that the true *Sonne* of rightwisenesse is risen aboue the *Horizon*, of our temporall *Hemisphærie*, and hath so abundantly streamed into our hartes, the direct beames of his goodnes, mercy, and grace: Whose heat All Creatures feele: Spirituall and Corporall: Visible and Inuisible. Shall we (I say) looke vpon the *Heauen*, *Sterres*, and *Planets*, as an Oxe and an Asse doth: no further carefull or inquisitiue, what they are: why were they Created, How do they execute that they were Created for? Seing, All Creatures, were for our sake created: and both we, and they,

Created, chiefly to glorifie the Almighty Creator: and that, by all meanes, to vs possible. *Nolite ignorare* (saith *Plato in Epinomis*) *Astronomiam, Sapientissimũ quiddam esse. Be ye not ignorant, Astronomie to be a thyng of excellent wisdom.* *Astronomie*, was to vs, from the beginning commended, and in maner commaunded by God him selfe. In asmuch as he made the *Sonne*, *Mone*, and *Sterres*, to be to vs, for *Signes*, and knowledge of Seasons, and for Distinctions of Dayes, and yeares. Many wordes nede not. But I wish, euery man should way this word, *Signes*. And besides that, conferre it also with the tenth Chapter of *Hieremie*. And though Some thinke, that there, they haue found a rod: Yet Modest Reason, will be indifferent Iudge, who ought to be beaten therewith, in respect of our purpose. Leauing that: I pray you vnderstand this: that without great diligence of Obseruation, examination and Calculation, their periods and courses (wherby *Distinction* of Seasons, yeares, and New Mones might precisely be knowne) could not exactly be certified. Which thing to performe, is that *Art*, which we here haue Defined to be *Astronomie*. Wherby, we may haue the distinct Course of Times, dayes, yeares, and Ages: aswell for Consideratiõ of Sacred Propheties, accomplished in due time, foretold: as for high Mysticall Solemnities holding: And for all other humane affaires, Conditions, and couenantes, vpon certaine time, betwene man and man: with many other great vses: Wherin, (verely), would be great incertainty, Confusion, vntruth, and brutish Barbarousnes: without the wonderfull diligence and skill of this Arte: continually learning, and determining Times, and periodes of Time, by the Record of the heauenly booke, wherein all times are written: and to be read with an *Astronomicall staffe*, in stede of a festue.

Musike, of Motion, hath his Originall cause: Therefore, after the motions most swift, and most Slow, which are in the Firmament, of Nature performed: and vnder the *Astronomers Consideration*: now I will Speake of an other kinde of *Motion*, producing sound, audible, and of Man numerable. *Musike* I call here that *Science*, which of the Grekes is called *Harmonice*. Not medling with the

Controuersie betwene the auncient *Harmonistes*, and *Canonistes*. Musike is a Mathematicall Science, which teacheth, by sense and reason, perfectly to iudge, and order the diuersities of soundes, hye and low. *Astronomie* and *Musike* are Sisters, saith *Plato*. As, for *Astronomie*, the eyes: So, for *Harmonious Motion*, the eares were made. But as *Astronomie* hath a more diuine Contemplation, and cōmodity, then mortall eye can perceiue: So, is *Musike* to be considered *Minde* may be preferred, before the eare. And from audible sound, we ought to ascende, to the examination: which numbers are *Harmonious*, and which not. And why, either, the one are: or the other are not. I could at large, in the *ethiops* and distances, describe a meruailous Harmonie, of *Pythagoras* with Eight stringes. Also, somewhat might be sayd of *Mechanicks*, eche of foure Stringes Elementall. And very straunge matter, might be alledged of the *Harmonie* *Spiritual* part appropriate. As in *Ptolomaus* third booke, in the fourth and sixth Chapters may appere. *It is the* cause of the apt bonde, and frendly felowship, of the Intellectuall and Mentall part of vs, with our grosse & corruptible body: but a certaine Meane, and *Harmonious Spirituality*, with both participatyng, & of both (in a maner) resultyng. *The* of Mans voyce, *the* also of Instrument, what might be sayd, of *Harmonie*: No common Musicien would lightly beleue.

I. D.

Read in Aristotle his 8. booke of Politikes: the 5, 6, and 7. chapters. Where you shall haue some occasion farder to thinke of Musike, than *But of the sundry Mixture* (as I may terme it) and concurse, diuerse collation, and Application of these *Harmonies*: as of thre, foure, fiue, or mo: Maruailous haue the effectes ben: and yet may be founde, and produced the like: with some proportionall consideration for our time, and being: in respect of the State, of the thinges then: in which, and by which, the wondrous effectes were wrought. *Democritus* and *Theophrastus* affirmed, that, by *Musike*, griefes and diseases of the Minde, and body might be cured, or inferred. And we finde in Recorde, that *Terpander*, *Arion*, *Ismenias*, *Orpheus*, *Amphion*, *Dauid*, *Pythagoras*, *Empedocles*, *Asclepiades*

and *Timotheus*, by *Harmonicall* Consonācy, haue done, and brought to pas, thinges, more then meruailous, to here of. Of them then, making no farder discourse, in this place: Sure I am, that Common *Musike*, commonly vsed, is found to the *Musiciens* and Hearers, to be so Commodious and pleasant, That if I would say and dispute, but thus much: That it were to be otherwise vsed, then it is, I should finde more repreeuers, then I could finde priuy, or skilfull of my meaning. In thinges therfore euident, and better knowen, then I can expresse: and so allowed and liked of, (as I would wish, some other thinges, had the like hap) I will spare to enlarge my lines any farder, but consequently follow my purpose.

Of Cosmographie, I appointed briefly in this place, to geue you some intelligence. Cosmographie, is the whole and perfect description of the heauenly, and also elementall parte of the world, and their homologall application, and mutuall collation necessarie. This Art, requireth *Astronomie*, *Geographie*, *Hydrographie* and *Musike*. Therefore, it is no small Arte, nor so simple, as in common practise, it is (slightly) considered. This matcheth Heauen, and the Earth, in one frame, and aptly applieth parts Correspōdent: So, as, the Heauenly Globe, may (in practise) be duely described vpon the Geographicall, and Hydrographicall Globe. And there, for vs to consider an *Æquinoctiall Circle*, an *Ecliptike line*, *Colures*, *Poles*, *Sterres* in their true Longitudes, Latitudes, Declinations, and Verticalitie: also Climes, and Parallels: and by an *Horizon* annexed, and reuolution of the earthly Globe (as the Heauen, is, by the *Primouant*, caried about in 24. æquall Houres) to learne the Risinges and Settings of *Sterres* (of *Virgill* in his *Georgikes*: of *Hesiod*: of *Hippocrates* in his *Medicinall Sphære*, to *Perdicca* King of the Macedonians: of *Diocles*, to King *Antigonus*, and of other famous *Philosophers* prescribed) a thing necessary, for due manuring of the earth, for *Nauigation*, for the Alteration of mans body: being, whole, Sicke, wounded, or brused. By the Reuolution, also, or mouing of the Globe Cosmographicall, the Rising and Setting of the Sonne: the

Lengthes, of dayes and nightes: the Houres and times (both night and day) are knowne: with very many other pleasant and necessary vses: Wherof, some are knowne: but better remaine, for such to know and ~~who~~ of a sparke of true fire, can make a wonderfull bonfire, by applying of due matter, duely.

Of Astrologie, here I make an Arte, seuerall from

Astronomie: not by new deuise, but by good reason and authoritie: for, Astrologie, is an Arte Mathematicall, which reasonably demonstrateth the operations and effectes, of the naturall beames, of light, and secrete influence: of the Sterres and Planets: in euery element and elementall body: at all times, in any Horizon assigned. This Arte is furnished with many other great Artes and experiences: As with perfecte *Perspectiue*, *Astronomie*, *Cosmographie*, *Naturall Philosophie* of the 4.

Elementes, the Arte of Graduation, and some good vnderstãding in *Musike*: and yet moreouer, with an other great Arte, hereafter following, though I, here, set this before, for some considerations me mouing. Sufficient (you see) is the stuffe, to make this rare and secrete Arte, of: and hard enough to frame to the Conclusion Syllogisticall. Yet both the manifolde and continuall trauailes of the most auncient and wise Philosophers, for the atteyning of this Arte: and by examples of effectes, to confirme the same: hath left vnto vs sufficient proufe and witnesse: and we, also, daily may perceauē, That mans body, and all other Elementall bodies, are altered, disposed, ordred, pleased, and displeased, by the Influentiall working of the *Sunne*, *Mone*, and the other Starres and Planets. And therefore, sayth *Aristotle*, in the first of his *Meteorologicall* bookes, in the second Chapter: *Est autem necessariò Mundus iste, supernis lationibus ferè continuus. Vt, inde, vis eius vniuersa regatur. Ea siquidem Causà prima putanda omnibus est, vnde motus principium existit.* That is: *This* [Elementall] *World is of necessitie, almost, next adioyning, to the heauenly motions: That, from thence, all his vertue or force may be gouerned. For, that is to be thought the first Cause*

vnto all: from which, the beginning of motion, is. And
 againe, in the tenth Chapter. *Oportet igitur & horum principia
 sumamus, & causas omnium similiter. Principium igitur vt
 mouens, præcipuum^{ue} & omnium primum, Circulus ille est, in
 quo manifeste Solis latio, &c.* And so forth. His *Meteorologicall*
 bookes, are full of argumentes, and effectuell demonstrations, of
 the vertue, operation, and power of the heauenly bodies, in and
 vpon the fower Elementes, and other bodies, of them (either
 perfectly, or vnperfectly) composed. And in his second booke, *De
 Generatione & Corruptione*, in the tenth Chapter. *Quocirca &
 prima latio, Ortus & Interitus causa non est: Sed obliqui Circuli
 latio: ea namq^{ue} & continua est, & duobus motibus fit:* In
 Englishe, thus. *Wherefore the vppermost motion, is not the
 cause of Generation and Corruption, but the motion of the
 Zodiake: for, that, both, is continuall, and is caused of two
 mouinges.* And in his second booke, and second Chapter of hys
Physikes. Homo namq^{ue} generat hominem, atq^{ue} Sol. For Man
 (sayth he) and the Sonne, are cause of mans generation.
 Authorities may be brought, very many: both of 1000. 2000. yea
 and 3000. yeares Antiquitie: of great *Philosophers, Expert, Wise,*
 and godly men, for that Conclusion: which, daily and hourelly, we
 men, may discerne and perceau by sense and reason: All beastes
 do feelee, and simply shew, by their actions and passions, outward
 and inward: All Plants, Herbes, Trees, Flowers, and Fruites. And
 finally, the Elementes, and all thinges of the Elementes composed,
 do geue Testimonie (as *Aristotle* sayd) that theyr *Whole
 Dispositions, vertues, and naturall motions, depend of the
 Actiuitie of the heauenly motions and Influences. Whereby,
 beside the specificall order and forme, due to euery seede:
 and beside the Nature, propre to the Indiuiduall Matrix, of
 the thing produced: What shall be the heauenly Impression,
 the perfect and circumspecte Astrologien hath to Conclude.*
 Not onely (by *Apotelesmes*) τὸ ὅτι. but by Naturall and

Mathematicall demonstration τὸ διότι. Whereunto, what Sciences are requisite (without exception) I partly haue here warned: And in my *Propædeumes* (besides other matter there disclosed) I haue Mathematically furnished vp the whole Method: To this our age, not so carefully handled by any, that euer I saw, or heard of. I was,

* Anno. 1548 and 1549. * In ~~1549~~ 21 ~~years~~ ago) by certaine earnest disputations, of the Learned *Gerardus Mercator*, and *Antonius Gogaua*, (and other,) therto so prouoked: and (by my constant and inuincible zeale to the veritie) in obseruations of Heauenly Influencies (to the Minute of time,) than, so diligent: And chiefly by the Supernaturall influence, from the Starre of Iacob, so directed: That any Modest and Sober Student, carefully and diligently seking for the Truth, will both finde & cōfesse, therin, to be the Veritie, of these my wordes: And also become a Reasonable Reformer, of three Sortes of people: about these Influentiall Operations, greatly erring from the truth, the ~~None~~ ^{One}, is Light Beleuers, the other, Light Despisers, and the third Light Practisers. The first, & most cōmon Sort, thinke the Heauen and Sterres, to be answerable to any their doubts, which is not so: and, in dede, they, to much, ouer reache. The Second sorte thinke no Influentiall vertue (frō the heauenly bodies) to beare any Sway in ~~Archetypion~~ ^{Creation}2, in this Elementall world. And to the *Sunne*, *Mone* and *Sterres* (being so many, so pure, so bright, so wonderfull bigge, so farre in distance, so manifold in their motions, so constant in their periodes. &c.) they assigne a sleight, simple office or two, and so allow vnto thē (according to their capacities) as much vertue, and power Influentiall, as to the Signe of the *Sunne*, *Mone*, and seuen Sterres, hanged vp (for Signes) in London, for distinction of houses, & such grosse helps, in our worldly affaires: And they vnderstand not (or will not vnderstand) of the other workinges, and vertues of the Heauenly *Sunne*, *Mone*, and *Sterres*: not so much, as the Mariner, or Husband man: no, not so much, as the *Elephant* doth, as the *Cynocephalus*, as the Porpentine doth: nor will allow these perfect, and incorruptible mighty bodies, so much vertuall Radiation, & Force, as they see in

a litle peece of a *Magnes stone*: which, at great distance, sheweth his operation. And perchance they thinke, the Sea & Riuers (as the Thames) to be some quicke thing, and so to ebbe, and flow, run in and out, of them selues, at their owne fantasies. God helpe, God helpe. Surely, these men, come to short: and either are to dull: or willfully blind: or, perhaps, to malicious. The third man, is the common and vulgare *Astrologien*, or Practiser: who, being not duely, artificially, and ~~improsedly~~ ^{improsedly} yet, either for vaine glory, or gayne: or like a simple dolt, & blinde Bayard, both in matter and maner, erreth: to the discredit of the *Wary*, and modest *Astrologien*: and to the robbing of those most noble corporall Creatures, of their Naturall Vertue: being most mighty: most beneficiall to all elementall Generation, Corruption and the appartenances: and most Harmonious in their Monarchie: For which thinges, being known, and modestly vsed: we might highly, and continually glorifie God, with the princely Prophet, saying. *The Heauens declare the Glorie of God: who made the Heauens in his wisdom: who made the Sonne, for to haue dominion of the day: the Mone and Sterres to haue dominion of the nyght: whereby, Day to day vttereth talke: and night, to night declareth knowledge. Prayse him, all ye Sterres, and Light. Amen.*

In order, now foloweth, of **Statike**, somewhat to say, what we meane by that name: and what commodity, doth, on such Art, depend. Statike, is an Arte Mathematicall, which demonstrateth the causes of heauynes, and lightnes of all thynges: and of motions and properties, to heauynes and lightnes, belonging. And for asmuch as, by the Bilanx, or Balance (as the chief sensible Instrument,) Experience of these demonstrations may be had: we call this Art, *Statike*: that is, *the Experimentes of the Balance*. Oh, that men wist, what proffit, (all maner of wayes) by this Arte might grow, to the hable examiner, and diligent practiser. “Thou onely, knowest all thinges precisely

(O God) who hast made weight and Balance, thy Iudgement: who hast created all thinges in *Number, Waight, and Measure*: and hast wayed the mountaines and hils in a Balance: who hast peysed in thy hand, both Heauen and earth. We therfore warned by the Sacred word, to Consider thy Creatures: and by that consideration, to wyne a glyms (as it were,) or shaddow of perceiuerance, that thy wisdom, might, and goodnes is infinite, and vnspeakable, in thy Creatures declared: And being farder aduertised, by thy mercifull goodnes, that, three principall wayes, were, of the, vsed in Creation of all thy Creatures, namely, *Number, Waight and Measure*, And for as much as, of *Number* and *Measure*, the two Artes (auncient, famous, and to humaine vses most necessary,) are, all ready, sufficiently knowen and extant: This third key, we beseeche thee (through thy accustomed goodnes,) that it may come to the nedefull and sufficient knowledge, of such thy Seruauntes, as in thy workemanship, would gladly finde, thy true occasions (purposely of the vsed) whereby we should glorifie thy name, and shew forth (to the weaklinges in faith) thy wondrous wisdom and Goodnes. Amen.

Meruaile nothing at this pang (godly frend, you Gentle and zelous Student.) An other day, perchaunce, you will perceiue, what occasion moued me. Here, as now, I will giue you some ground, and withall some shew, of certaine commodities, by this Arte arising. And bycause this Arte is rare, my wordes and practises might be to darke: vnleast you had some light, holden before the matter: and that, best will be, in giuing you, out of *Archimedes* demonstrations, a few principal Conclusions, as foloweth.

1.

The Superficies of euery Liquor, by it selfe consistyng, and in quyet, is Sphæricall: the centre whereof, is the same, which is the centre of the Earth.

2.

If Solide Magnitudes, being of the same bignes, or quãtitie, that any Liquor is, and hauyng also the same Waight: be let downe into the same Liquor, they will settle downeward, so, that no parte of them, shall be aboue the Superficies of the Liquor: and yet neuertheles, they will not sinke vtterly downe, or drowne.

3.

If any Solide Magnitude beyng Lighter then a Liquor, be let downe into the same Liquor, it will settle downe, so farre into the same Liquor, that so great a quantitie of that Liquor, as is the parte of the Solid Magnitude, settled downe into the same Liquor: is in Waight, æquall, to the waight of the whole Solid Magnitude.

4.

Any Solide Magnitude, Lighter then a Liquor, forced downe into the same Liquor, will moue vpward, with so great a power, by how much, the Liquor hauyng æquall quantitie to the whole Magnitude, is heauyer then the same Magnitude.

5.

Any Solid Magnitude, heauyer then a Liquor, beyng let downe into the same Liquor, will sinke downe vtterly: And wilbe in that Liquor, Lighter by so much, as is the waight or heauynes of the Liquor, hauing bygnes or quantitie, æquall to the Solid Magnitude.

6.

I. D.

The Cutting of a Sphære according to any proportion assigned may by this proposition

be done Mechanically by tempering Liquor to a certayne waight in respect of the waight of the Sphære therein Swymming.

If any Solide Magnitude, Lighter then a Liquor, be let downe into the same Liquor, the waight of the same Magnitude, will be, to the Waight of the Liquor. (Which is æquall in quantitie to the whole Magnitude,) in that proportion, that the parte, of the Magnitude settled downe, is to the whole Magnitude.

BY these verities, great Errors may be reformed, in Opinion of the Naturall Motion of thinges, Light and Heauy. Which errors, are in Naturall Philosophie (almost) of all mē allowed: to much trusting to Authority: and false Suppositions. As, Of any two bodyes, the heauyer, to moue downward faster then the lighter. ~~This error, is not~~ *A common* first by me, Noted: but by one *Iohn Baptist de Benedictis*. The chief of his propositions, is this: which seemeth a Paradox.

A paradox.

If there be two bodyes of one forme, and of one kynde, æquall in quantitie or vnæquall, they will moue by æquall space, in æquall tyme: So that both theyr mouynges be in ayre, or both in water: or in any one Middle.

Hereupon, in the ~~Common~~ *Canonyng*, Veraine good discourses (otherwise) may receiue great amendement, and furdurance. *The wonderfull vse of these Propositiones*. In the ~~proposed~~ purpose, also, allowing somewhat to the imperfection of Nature: not aunswerable to the precisenes of demonstration. Moreouer, by the foresaid propositions (wisely vsed.) The Ayre, the water, the Earth, the Fire, may be nerely, knowen, how light or heauy they are (Naturally) in their assigned partes: or in the whole. And then, to thinges Elementall, turning your practise: you may deale for the proportion of the Elementes, in the thinges Compounded. Then, to the proportions of the Humours in Man: their waighes: and the waight of his bones, and

flesh. &c. Than, by waight, to haue consideration of the Force of man, any maner of way: in whole or in part. Then, may you, of Ships water drawing, diuersly, in the Sea and in fresh water, haue pleasant consideration: and of waying vp of any thing, sonken in Sea or in fresh water &c. And (to lift vp your head a loft:) by waight, you may, as precisely, as by any instrument els, measure the Diameters of *Sonne* and *Mone*. &c. Frende, I pray you, way these thinges, with the iust Balance of Reason. And you will finde Meruailes vpon Meruailes: And esteme one Drop of Truth (yea in Naturall Philosophie) more worth, then whole Libraries of Opinions, vndemonstrated: or not aunswering to Natures Law, and your experience. Leauing these thinges, thus: I will giue you two or three, light practises, to great purpose: and so finish my Annotation *Staticall*. In Mathematicall matters, by the Mechaniciens ayde, we will behold, here, the Commodity of waight. *The practise Staticall, to know the proportion, betwene the Cube, ~~Make the Sphere~~ of any one Vniforme: and through like heauy stuffe: of the same Stuffe, make a Sphære or Globe, precisely, of a Diameter æquall to the Radicall side of the Cube. Your stuffe, may be wood, Copper, Tinne, Lead, Siluer. &c. (being, as I sayd, of like nature, condition, and like waight throughout.) And you may, by Say Balance, haue prepared a great number of the smallest waightes: which, by those Balance can be discerned or tryed: and so, haue proceded to make you a perfect Pyle, company & Number of waightes: to the waight of six, eight, or twelue pound waight: most diligently tryed, all. And of euery one, the Content knowen, in your least waight, that is wayable. [They that can not haue these waightes of precisenes: may, by Sand, Vniforme, and well dusted, make them a number of waightes, somewhat nere precisenes: by halving euer the Sand: they shall, at length, come to a least common waight. Therein, I leaue the farder matter, to their discretion, whom nede shall pinche.] The *Venetians* consideration of waight, may seme precise enough: by eight descentes progressionall,* * *I. D.* For, so, haue you .256. parts of a ~~hundred~~ *Graine* grayne. Your Cube, Sphære, apt Balance, and conuenient waightes, being ready: fall to*

worke.*. First, way your Cube. Note the Number of the waight.
 Way, after that, your Sphære. Note likewise, the Nũber of the
 waight. If you now find the waight of your Cube, to be to the
 waight of the Sphære, as 21. is to 11: Then you see, how the
 Mechanicien and *Experimenter*, without Geometrie and
 Demonstration, are (as nerely in effect) taught the proportion of
 the Cube to the Sphere: as I haue demonstrated it, in the end of the
 twelfth boke of *Euclide*. Often, try with the same Cube and
 Sphære. Then, chaunge, your Sphære and Cube, to an other matter:
 or to an other bignes: till you haue made a perfect vniuersall
 Experience of it. Possible it is, that you shall wyne to nerer
 termes, in the proportion.

When you haue found this one certaine Drop of Naturall veritie,
 procede on, to Inferre, and duely to make assay, of matter
 depending. As, bycause it is well demonstrated, that a Cylinder,
 whose heith, and Diameter of his base, is æquall to the Diameter
 of the Sphære, is Sesquialter to the same Sphære (that is, as 3. to
 2:) To the number of the waight of the Sphære, adde halfe so
 much, as it is: and so haue you the number of the waight of that
 Cylinder. Which is also Comprehended of our former Cube: So,
 that the base of that Cylinder, is a Circle described in the Square,
 which is the base of our Cube. But the Cube and the Cylinder,
 being both of one heith, haue their Bases in the same proportion,
 in the which, they are, one to an other, in their Massines or
 Soliditie. But, before, we haue two numbers, expressing their
 Massines, Solidities, and Quantities, by waight: wherfore, we haue

* *The proportion of the Square to the Circle.* * *the proportion of the Square, to the*
 Circle, inscribed in the same Square. And so are we fallen into the
 knowledge sensible, and Experimentall of *Archimedes* great
 Secret: of him, by great trauaile of minde, sought and found.

Wherfore, to any Circle giuen, you can giue a Square æquall: *

* *as I haue taught, in my Annotation, vpon the first*
proposition of the twelfth boke, And likewise, to any Square giuen,
 you may giue a Circle æquall: * *To any Square geuen, to geue a Circle,*

~~square~~ a Circle, which shall be in that proportion, to your Circle

inscribed, as the Square is to the same Circle: This, you may do,
 by my Annotations, vpon the second proposition of the twelfth
 booke of *Euclide*, in my third Probleme there. Your diligence may
 come to a proportion, of the Square to the Circle inscribed, nerer
 the truth, then is the proportion of 14. to 11. And consider, that you
 may begyn at the Circle and Square, and so come to conclude of
 the Sphære, & the Cube, what their proportion is: as now, you
 came from the Sphære to the Circle. For, of Siluer, or Gold, or
 Latton Lamyns or plates (thorough one hole drawẽ, as the maner
 is) if you make a Square figure & way it: and then, describing
 thereon, the Circle inscribed: & cut of, & file away, precisely (to the
 Circle) the ouerplus of the Square: you shall then, waying your
 Circle, see, whether the waight of the Square, be to your Circle, as
 14. to 11. As I haue Noted, in the beginning of *Euclides* twelfth
 booke. &c. after this resort to my last proposition, vpon the last of
 the twelfth. And there, helpe your selfe, to the end. And, here,
 Note this, by the way. *Note Squaring of the Circle without
 knowledge of the proportion betwene Circumference and
 Diameter.* Square the Circle, without hauing knowledge of the
 proportion, of the Circumference to the Diameter: as you haue
 here perceiued. And otherwayes also, I can demonstrate it. So that,
 many haue cumberd them selues superfluously, by trauailing in
 that point first, which was not of necessitie, first: and also very
 intricate. And easily, you may, (and that diuersly) come to the
 knowledge of the Circumference: the Circles Quantitie, being first
 knowen. Which thing, I leaue to your consideration: making hast
 to despatch an other Magistrall Probleme: and to bring it, nerer to
 your knowledge, and readier dealing with, then the world (before
 this day,) had it for you, that I can tell of. And that is, *A
 Mechanicall Dubblyng of the Cube: &c.* Which may, thus, be
 done: *To Dubble the Cube redily: by Art Mechanicall:
 depending vppon Demonstration.* Make of Copper plates, or Tyn
 plates, a foursquare vpright Pyramis, or a Cone: perfectly
 fashioned in the holow, within. Wherin, let great diligence
 be vsed, to approche (as nere as may be) to the

Mathematicall perfection of those figures. At their bases, let them be all open: euery where, els, most close, and iust to. From the vertex, to the Circumference of the base of the Cone: & to the sides of the base of the Pyramis: I. D.

The 4. sides of this Pyramis must be 4. Isosceles Triangles Let 4. straight lines be drawen, in the inside of the Cone and Pyramis: making at their fall, on the perimeters of the bases, equall angles on both sides them selues, with the sayd perimeters. These 4. lines (in the Pyramis: and as many, in the Cone) diuide: one, in 12. æquall partes: and an other, in 24. an other, in 60, and an other, in 100. (rekenyng vp from the vertex.) Or vse other numbers of diuision, as experience shall teach you. Then,* I. D.

** In all workinges with this Pyramis or Cone, Let their Situations be in all Pointes and Conditions, alike, or all one: while you are about one Work* Set your Cone or Pyramis, with the vertex downward, perpendicularly, in respect of the Base. (Though it be otherwayes, it hindreth nothyng.) So let thẽ most stedily be stayed. Now, if there be a Cube, which you wold haue Dubbled. Make you a prety Cube of Copper, Siluer, Lead, Tynne, Wood, Stone, or Bone. Or els make a hollow Cube, or Cubik coffen, of Copper, Siluer, Tynne, or Wood &c. These, you may so proportiõ in respect of your Pyramis or Cone, that the Pyramis or Cone, will be hable to contene the waight of them, in water, 3. or 4. times: at the least: what stuff so euer they be made of. Let not your Solid angle, at the vertex, be to sharpe: but that the water may come with ease, to the very vertex, of your hollow Cone or Pyramis. Put one of your Solid Cubes in a Balance apt: take the waight therof exactly in water. Powre that water, (without losse) into the hollow Pyramis or Cone, quietly. Marke in your lines, what numbers the water Cutteth: Take the waight of the same Cube againe: in the same kinde of water, which you had before: put that* also, I. D.

** Consider well whan you must put your waters togyther: and whan, you must empty your first water, out of your Pyramis or Cone* into the Pyramis or Cone, where

you did put the first. Marke now againe, in what number or place
 of the lines, the water Cutteth them. Two wayes you may conclude
 your purpose: it is to wete, either by numbers or lines. By
 numbers: as, if you diuide the side of your Fundamentall Cube into
 so many æquall partes, as it is capable of, conueniently, with your
 ease, and precisenes of the diuision. For, as the number of your
 first and lesse line (in your hollow Pyramis or Cone,) is to the
 second or greater (both being counted from the vertex) so shall the
 number of the side of your Fundamentall Cube, be to the nūber
 belonging to the Radicall side, of the Cube, dubble to your
 Fundamentall Cube: Which being multiplied Cubik wise, will sone
 shew it selfe, whether it be dubble or no, to the Cubik number of
 your Fundamentall Cube. By lines, thus: As your lesse and first
 line, (in your hollow Pyramis or Cone,) is to the second or greater,
 so let the Radical side of your Fundamētall Cube, be to a fourth
 proportionall line, by the 12. proposition, of the sixth boke of
Euclide. Which fourth line, shall be the Rote Cubik, or Radicall
 side of the Cube, dubble to your Fundamentall Cube: which is the
 thing we desired *God be thanked for this Inuention, & the fruite*
~~sayng~~ *sayng* (with ioy) say, EYPHKA, EYPHKA, EYPHKA: thanking
 the holy and glorious Trinity: hauing greater cause therto, then *
Vitruuius. Archimedes had (for finding the fraude vsed in the
 Kinges Crowne, of Gold): as all men may easily Iudge: by the
 diuersitie of the frute following of the one, and the other. Where I
 spake before, of a hollow Cubik Coffen: the like vse, is of it: and
 without waight. Thus. Fill it with water, precisely full, and poure
 that water into your Pyramis or Cone. And here note the lines
 cutting in your Pyramis or Cone. Againe, fill your coffen, like as
 you did before. Put that Water, also, to the first. Marke the second
 cutting of your lines. Now, as you proceded before, so must you
 here proceed. ~~And if the Cube~~ *And if the Cube*, which you should Double, be neuer so
 great: you haue, thus, the proportion (in small) betwene your two
 litle Cubes: And then, the side, of that great Cube (to be doubled)
 being the third, will haue the fourth, found, to it proportionall: by
 the 12. of the sixth of *Euclide*.

Note, as concerning the Sphæricall Superficie of that Altitude while, I forget not my first Proposition Staticall, here rehearsed: that, the Superficies of the water, is Sphæricall. Wherein, vse your discretion: to the first line, adding a small heare breadth, more: and to the second, halfe a heare breadth more, to his length. For, you will easily perceauē, that the difference can be no greater, in any Pyramis or Cone, of you to be handled. Which you shall thus trye.

For finding the swelling of the water about the leuell. Square the Semidiameter, from the Centre of the earth, to your first Waters Superficies. Square then, halfe the Subtendent of that watry Superficies (which Subtendent must haue the equall partes of his measure, all one, with those of the Semidiameter of the earth to your watry Superficies): Subtracte this square, from the first: Of the residue, take the Rote Square. That Rote, Subtracte from your first Semidiameter of the earth to your watry Superficies: that, which remaineth, is the heith of the water, in the middle, about the leuell. Which, you will finde, to be a thing insensible. And though it were greatly sensible, by help of my sixt Theoreme vpon the last Proposition of Euclides twelfth booke, noted: you may reduce all, to a true Leuell. But, farther diligence, of you is to be vsed, against accidentall causes of the waters swelling: as by hauing (somwhat) with a moyst Sponge, before, made moyst your hollow Pyramis or Cone, will preuent an accidentall cause of Swelling, &c. Experience will teach you abundantly: with great ease, pleasure, and cōmoditie.

Thus, may you Double the Cube Mechanically, Treble it, and so forth, in any proportion. *Note this Abridgement of Dubbling the Cube.* Abridge your paine, cost, and Care herein. Without all preparing of your Fundamentall Cubes: you may (alike) worke this Conclusion. For, that, was rather a kinde of Experimentall demõstration, then the shortest way: and all, vpon one Mathematicall Demonstration depending. “Take water (as much as conueniently will serue your turne: as I warned before of your Fundamentall Cubes bignes) Way it precisely. Put that water, into

your Pyramis or Cone. Of the same kinde of water, then take againe, the same waight you had before: put that likewise into the Pyramis or Cone. For, in eche time, your marking of the lines, how the Water doth cut them, shall geue you the proportion betwen the Radicall sides, of any two Cubes, wherof the one is Double to the other: working as before I haue taught you that for ~~you~~ ^{*Noo} Fundamentall Cube his Radicall side: here, you may take a right line, at pleasure”.

Yet farther proceeding with our droppe of Naturall truth: *To giue Cubes one to the other in any proportion, Rationally* ~~your may (now)~~ geue Cubes, one to the other, in any proportiō geuē:

Rationall or Irrationall: on this maner. Make a hollow Parallelipipedon of Copper or Tinne: with one Base wāting, or open: as in our Cubike Coffen. Frō the bottome of that Parallelipipedon, raise vp, many perpendiculars, in euery of his fower sides. Now if any proportion be assigned you, in right lines: Cut one of your perpendiculars (or a line equall to it, or lesse then it) likewise: by the 10. of the sixth of Euclide. And those two partes, set in two sundry lines of those perpendiculars (or you may set them both, in one line) making their beginninges, to be, at the base: and so their lengthes to extend vpward. Now, set your hollow Parallelipipedon, vpright, perpendicularly, steadie. Poure in water, handsomly, to the heith of your shorter line. Poure that water, into the hollow Pyramis or Cone. Marke the place of the rising. Settle your hollow Parallelipipedon againe. Poure water into it: vnto the heith of the second line, exactly. Poure that water* **Emptying* ~~the first~~ ^{into the first} hollow Pyramis or Cone: Marke now againe, where the water cutteth the same line which you marked before. For, there, as the first marked line, is to the second: So shall the two Radicall sides be, one to the other, of any two Cubes: which, in their Soliditie, shall haue the same proportion, which was at the first assigned: were it Rationall or Irrationall.

Thus, in sundry waies you may furnishe your selfe with such straunge and profitable matter: which, long hath bene wished for.

And though it be Naturally done and Mechanically: yet hath it a good Demonstration Mathematicall. *The demonstrations of this Dubbling of the Which is this.* Alwaies, you haue two Like Pyramids: or two Like Cones, in the proportions assigned: and like Pyramids or Cones, are in proportion, one to the other, in the proportion of their Homologall sides (or lines) tripled. Wherefore, if to the first, and second lines, found in your hollow Pyramis or Cone, you ioine a third and a fourth, in continuall proportion: that fourth line, shall be to the first, as the greater Pyramis or Cone, is to the lesse: by the 33. of the eleuenth of Euclide. If Pyramis to Pyramis, or Cone to Cone, be double, then shall* *I. D.*

** Hereby, helpe your self to become a præcise practiser. And so consider, how, nothing at all, you are hindred (sensibly) by the* ~~Line to Line~~ *Line to Line, be also double, &c.*

But, as our first line, is to the second, so is the Radicall side of our Fundamentall Cube, to the Radicall side of the Cube to be made, or to be doubled: and therefore, to those twaine also, a third and a fourth line, in continuall proportion, ioyned: will geue the fourth line in that proportion to the first, as our fourth Pyramidall, or Conike line, was to his first: but that was double, or treble, &c. as the Pyramids or Cones were, one to an other (as we haue proued) therefore, this fourth, shalbe also double or treble to the first, as the Pyramids or Cones were one to an other: But our made Cube, is described of the second in proportion, of the fower proportionall lines: therefore* ** By the 33. of the eleuenth of Euclide,* as the fourth line, is to the first, so is that Cube, to the first Cube: and we haue proued the fourth line, to be to the first, as the Pyramis or Cone, is to the Pyramis or Cone: Wherefore the Cube is to the Cube, as Pyramis is to Pyramis, or Cone is to Cone. But we* *I. D.*

** And your diligence in practise, can so (in waight of water) performe it: Therefore, now, you are able to geue good reasons* ~~Suppose Pyramis to Pyramis, or Cone to~~

~~Cone, to be double or treble. &c. Therefore Cube, is to Cube, double, or treble, &c. Which was to be demonstrated. And of the~~ Parallelipipedō, it is euidēt, that the water Solide Parallelipipedons, are one to the other, as their heithes are, seing they haue one base. Wherefore the Pyramids or Cones, made of those water Parallelipipedons, are one to the other, as the lines are

(one to the other) betwene which, our proportion was assigned. But the Cubes made of lines, after the proportiō of the Pyramidal or Conik *homologall* lines, are one to the other, as the Pyramides or Cones are, one to the other (as we before did proue) therefore, the Cubes made, shalbe one to the other, as the lines assigned, are one to the other: Which was to be demonstrated. Note. * *Note* ~~This, may Demon~~stratiō is more generall, then onely in Square Pyramis or Cone: Consider well. Thus, haue I, both Mathematically and Mechanically, ben very long in wordes: yet (I trust) nothing tedious to them, who, to these thinges, are well affected. And verily I am forced (auoiding prolixitie) to omit sundry such things, easie to be practised: which to the Mathematicien, would be a great Threasure: and to the Mechanicien, no small gaine. * *The great Commodities following of these* ~~Now I mention~~ *Now I mention*, Betwene two lines giuen, finde two middle proportionals, in Continuall proportion: by the hollow Parallelipedon, and the hollow Pyramis, or Cone. Now, any Parallelipedon rectangle being giuen: thre right lines may be found, proportionall in any proportion assigned, of which, shal be produced a Parallelipedon, æquall to the Parallelipedon giuen. Hereof, I noted somewhat, vpon the 36. proposition, of the 11. boke of *Euclide*. Now, all those thinges, which *Vitruuius* in his Architecture, specified hable to be done, by dubbling of the Cube: Or, by finding of two middle proportionall lines, betwene two lines giuen, may easely be performed. Now, that Probleme, which I noted vnto you, in the end of my Addition, vpon the 34. of the 11. boke of *Euclide*, is proued possible. Now, may any regular body, be Transformed into an other, &c. Now, any regular body: any Sphere, yea any Mixt Solid: and (that more is) Irregular Solides, may be made (in any proportiō assigned) like vnto the body, first giuen. Thus, of a *Manneken*, (as the *Dutch* Painters terme it) in the same *Symmetrie*, may a Giant be made: and that, with any gesture, by the *Manneken* vsed: and contrarywise. Now, may you, of any Mould, or Modell of a Ship, make one, of the same Mould (in any assigned proportion) bigger

or lesser. Now, may you, of ~~a~~^{any} Gunne, or little peece of ordinaũce, make an other, with the same *Symmetrie* (in all pointes) as great, and as little, as you will. Marke that: and thinke on it. Infinitely, may you apply this, so long sought for, and now so easily concluded: and withall, so willingly and frankly communicated to such, as faithfully deale with vertuous studies. *Such is the Fruite of the Mathematicall Sciences and the Mathematicall minde*, deale Speculatiuely in his own Arte: and by good meanes, Mount aboue the cloudes and sterres: And thirdly, he can, by order, Descend, to frame Naturall thinges, to wonderfull vses: and when he list, retire home into his owne Centre: and there, prepare more Meanes, to Ascend or Descend by: and, all, to the glory of God, and our honest delectation in earth.

Although, the Printer, hath looked for this Præface, a day or two, yet could I not bring my pen from the paper, before I had giuen you comfortable warning, and brief instructions, of some of the Commodities, by *Statike*, hable to be reaped: In the rest, I will therefore, be as brief, as it is possible: and with all, describing them, somewhat accordingly. And that, you shall perceiue, by this, which in order commeth next. For, wheras, it is so ample and wonderfull, that, an whole yeare long, one might finde fruitfull matter therein, to speake of: and also in practise, is a Treasure endeles: yet will I glanse ouer it, with wordes very few.

THis do I call **Anthropographie**. Which is an Art restored, and of my preferment to your Seruice. I pray you, thinke of it, as of one of the chief pointes, of Humane knowledge. Although it be, but now, first Cõfirmed, with this new name: yet the matter, hath from the beginning, ben in consideration of all perfect Philosophers. **Anthropographie**, is the description of the Number, Measure, Waight, figure, Situation, and colour of euery diuerse thing, conteyned in the perfect body of MAN: with certain knowledge of the Symmetrie, figure, waight, Characterization, and due locall motion, of any

parcell of the sayd body, assigned: and of Nũbers, to the sayd parcell appertainyng. This, is the one part of the Definition, mete for this place: Sufficient to notifie, the particularitie, and excellency of the Arte: and why it is, here, ascribed to the Mathematics. Yf the description of the heauenly part of the world, had a peculier Art, called *Astronomie*: If the description of the earthly Globe, hath his peculier arte, called *Geographie*. If the Matching of both, hath his peculier Arte, called *Cosmographie*: Which is the Descriptiõ of the whole, and vniuersall frame of the world: Why should not the description of

~~MAN is *Microcosmus*, who *Macrocosmus*~~ *MAN* is *Microcosmus*, who *Macrocosmus*. Lesse world: and, frõ the beginning, called *Microcosmus* (that is. *The Lesse World*.) And for whose sake, and seruice, all bodily creatures els, were created: Who, also, participateth with Spirites, and Angels: and is made to the Image and similitude of *God*: haue his peculier Art? and be called the *Arte of Artes*: rather, then, either to want a name, or to haue to base and improprie a name? You must of sundry professions, borow or challenge home, peculier partes hereof: and farder procede: as, God, Nature, Reason and Experience shall informe you. The Anatomistes will restore to you, some part: The Physiognomistes, some: The Chyromantistes some. The Metaposcopistes, some: The excellent, *Albert Durer*, a good part: the Arte of Perspectiue, will somewhat, for the Eye, helpe forward: *Pythagoras*, *Hipocrates*, *Plato*, *Galenus*, *Meletius*, & many other (in certaine thinges) will be Contributaries. And farder, the Heauen, the Earth, and all other Creatures, will eche shew, and offer their Harmonious seruice, to fill vp, that, which wanteth hereof: and with your own Experience, concluding: you may Methodically register the whole, for the posteritie: Whereby, good profe will be had, of our Harmonious, and ~~*Microcosmus*~~ *Microcosmus*. constitutiõ. The outward Image, and vew hereof: to the Art of *Zographie* and Painting, to Sculpture, and Architecture: (for Church, House, Fort, or Ship) is most necessary and profitable: for that, it is the chiefe base and foundation of them. Looke in ~~*Libus in Cap.*~~ **Libus in Cap.* whether I deale sincerely for your behoufe, or no. Looke in *Albertus Durerus, De Symmetria humani*

Corporis. Looke in the 27. and 28. Chapters, of the second booke, *De occulta Philosophia*. Consider the *Arke* of *Noe*. And by that, wade farther. Remember the *Delphicall Oracle NOSCE TEIPSVM* (*Knowe thy selfe*) so long agoe pronounced: of so many a Philosopher repeated: and of the *Wisest* attempted: And then, you will perceauce, how long agoe, you haue bene called to the Schole, where this Arte might be learned. Well. I am nothing affrayde, of the disdayne of some such, as thinke Sciences and Artes, to be but Seuen. Perhaps, those Such, may, with ignorance, and shame enough, come short of them Seuen also: and yet neuerthelesse they can not prescribe a certaine number of Artes: and in eche, certaine vnpassable boundes, to God, Nature, and mans Industrie. New Artes, dayly rise vp: and there was no such order taken, that all Artes, should in one age, or in one land, or of one man, be made knowne to the world. Let vs embrace the giftes of God, and wayes to wisdom, in this time of grace, from aboue, continually bestowed on them, who thankfully will receiue them: *Et bonis Omnia Cooperabuntur in bonum*.

Trochilike, is that Art Mathematicall, which demonstrateth the properties of all Circular motions, Simple and Compounde. And bycause the frute hereof, vulgarly receiued, is in Wheles, it hath the name of *Trochilike*: as a man would say, *Whele Art*. By this art, a Whele may be geuen which shall moue ones about, in any tyme assigned. Two Wheles may be giuen, whose turnynges about in one and the same tyme, (or equall tymes), shall haue, one to the other, any proportion appointed. By Wheles, may a straight line be described: Likewise, a Spirall line in plaine, Conicall Section lines, and other Irregular lines, at pleasure, may be drawen. These, and such like, are principall Conclusions of this Arte: and helpe forward many pleasant and profitable Mechanicall workes. As Milles, Mill/Saw great and very long Deale bordes, no man being by. Such haue I seene in Germany: and in the Citie of Prage: in the kingdome of Bohemia: Coyning Milles, Hand Milles for Corne grinding: And all maner of

Milles, and Whele worke: By Winde, Smoke, Water, Waight, Spring, Man or Beast, moued. Take in your hand, *Agricola De re Metallica*: and then shall you (in all Mines) perceau, how great nede is, of Whele worke. By Wheles, straunge workes and incredible, are done: as will, in other Artes hereafter, appeare. A wonderfull example of farther possibilitie, and present commoditie, was sene in my time, in a certaine Instrument: which by the Inuenter and Artificer (before) was solde for xx. Talentes of Golde: and then had (by misfortune) receaued some iniurie and hurt: And one *Ianellus* of *Cremona* did mend the same, and presented it vnto the Emperour *Charles* the fifth. *Hieronymus Cardanus*, can be my witnesse, that therein, was one Whele, which moued, and that, in such rate, that, in 7000. yeares onely, his owne periode should be finished. A thing almost incredible: But how farre, I keepe me within my boundes: very many men (yet aliue) can tell.

Helicosophie, is nere Sister to *Trochilike*: and is, An Arte Mathematicall, which demonstrateth the designing of all Spirall lines in Plaine, on Cylinder, Cone, Sphære, Conoid, and Sphæroid, and their properties appertayning. The vse hereof, in *Architecture*, and diuerse Instrumentes and Engines, is most necessary. For, in many thinges, the Skrue worketh the feate, which, els, could not be performed. By helpe hereof, it is * *Athenes* recorded, that, where all the power of the Citie of *Syracusa*, was not hable to moue a certaine Ship (being on ground) mightie *Archimedes*, setting to, his Skruish Engine, caused *Hiero* the king, by him self, at ease, to remoue her, as he would.

~~When the King~~ *When the King* wondring: Από τάντης τῆς ἡμέρας, περί παντός, Αρχιμήδει λέγοντι πιςευτέομ. *From this day, forward* (said the King) *Credit ought to be giuen to Archimedes, what soeuer he sayth.*

Pneumatithmie demonstrateth by close hollow Geometricall Figures, (regular and irregular) the straunge

properties (in motion or stay) of the Water, Ayre, Smoke, and Fire, in theyr cōtinuitie, and as they are ioyned to the Elementes next them. This Arte, to the Naturall Philosopher, is very proffitable: to proue, that *Vacuum*, or *Emptines* is not in the world. And that, all Nature, abhorreth it so much: that, contrary to ordinary law, the Elementes will moue or stand. As, Water to ascend: rather then betwene him and Ayre, Space or place should be left, more then (naturally) that quātitie of Ayre requireth, or can fill. Againe, Water to hang, and not descend: rather then by descending, to leaue Emptines at his backe. The like, is of Fire and Ayre: they will descend: when, either, their Cōtinuitie should be dissolued: or their next Element forced from them. And as they will not be extended, to discontinuitie: So, will they not, nor yet of mans force, can be prest or pent, in space, not sufficient and aunswerable to their bodily substance. Great force and violence will they vse, to enioy their naturall right and libertie. *To go to the bottom of the Sea without danger* or three men together, by keping Ayre vnder a great Cauldron, and forcyng the same downe, orderly, may without harme descend to the Sea bottome: and continue there a tyme &c. Where, Note, how the thicker Element (as the Water) giueth place to the thynner (as, is the ayre:) and receiueh violence of the thinner, in maner. &c. Pumps and all maner of Bellowes, haue their ground of this Art: and many other straunge deuises. As, *Hydraulica*, Organes goyng by water. &c. Of this Feat, (called commonly *Pneumatica*,) goodly workes are extant, both in Greke, and Latin. With old and learned Schole men, it is called *Scientia de pleno & vacuo*.

Menadrie, is an Arte Mathematicall, which demonstrateth, how, aboue Natures vertue and power simple: Vertue and force may be multiplied: and so, to direct, to lift, to pull to, and to put or cast fro, any multiplied or simple, determined Vertue, Waight or Force: naturally, not, so, directible or moueable. Very much is this Art furdred by other Artes: as, in some pointes, by *Perspectiue*: in

some, by *Statike*: in some, by *Trochilike*: and in other, by
Helicosophie: and *Pneumatithmie*. By this Art, all Cranes,
 Gybbettes, & Ingines to lift vp, or to force any thing, any maner
 way, are ordred: and the certaine cause of their force, is knowne:
 As, the force which one man hath with the Duche waghen Racke:
 therwith, to set vp agayne, a mighty waghen laden, being
 ouerthrowne. The force of the Crossebow Racke, is certainly, here,
 demonstrated. The reason, why one mā, doth with a leauer, lift
 that, which Sixe men, with their handes onely, could not, so easily
 do. By this Arte, in our common Cranes in London, where powre
 is to Crane vp, the waight of 2000. pound: by two Wheles more
 (by good order added) Arte concludeth, that there may be Craned
 vp 200000. pound waight &c. So well knew *Archimedes* this Arte:
 that he alone, with his deuises and engynes, (twise or thrise)
 spoyled and discomfited the whole Army and Hoste of the
 Romaines, besieging *Syracusa*, *Plutarchus* ~~Marcus Marcellus~~ the
Consul, being their Generall Capitaine. Such huge Stones, so
 many, with such force, and so farre, did he with his engynes hayle
 among the Sea, and the City, that though their Ships might come to the
 walls of *Syracusa*, yet hee vtterly confounded the Romaine Nauye.
 What with his mighty Stones hurlyng: what with Pikes of* *
 long, made like shaftes: which he forced almost a quarter of a myle.
 What, with his catchyng hold of their Shyps, and hoysing them vp
 aboue the water, and suddenly letting them fall into the Sea againe:
 what with his *Glasses*, by which he fired their other Shippes a far-of:
 what, with his other pollicies, deuises, and engines, he so manfully
 acquit him selfe: that all the Force, courage, and pollicie of the
 Romaines (for a great season) could nothing preuaile, for the
 winning of *Syracusa*. Wherupon, the Romanes named *Archimedes*,
Briareus, and *Centimanus*. *Zonaras* maketh mention of one
Proclus, who so well had perceiued *Archimedes* Arte of *Menadrie*,
 and had so well inuented of his owne, that with his Burning
 Glasses, ~~Being placed~~ upon the walles of *Bysance*, he
 multiplied so the heate of the Sunne, and directed the beames of
 the same against his enemies Nauie with such force, and so
 sodeinly (like lightening) that he burned and destroyed both man

and ship. And *Dions* specieth of *Priscus*, a *Geometricien* in Bysance, who inuented and vsed sondry Engins, of Force multiplied: Which was cause, that the *Emperour Seuerus* pardoned him, his life, after he had wonne Bysance: Bycause he honored the Arte, wytt, and rare industrie of *Priscus*. But nothing inferior to the inuention of these engins of Force, was the inuention of Gunnes, which, ~~German~~ English man, had the occasion and order of first inuenting: though in an other land, and by other men, it was first executed. And they that should see the record, where the occasion and order generall, of Gunning, is first discoursed of, would thinke: that, “small thinges, slight, and cōmon: comming to wise mens consideration, and industrious mens handling, may grow to be of force incredible.”

Hypogeiodie, is an Arte Mathematicall, demonstratyng, how, vnder the Sphæricall Superficies of the earth, at any depth, to any perpendicular line assigned (whose distance from the perpendicular of the entrance: and the Azimuth, likewise, in respect of the said entrance, is knowen) certaine way may be præscribed and gone: And how, any way aboue the Superficies of the earth designed, may vnder earth, at any depth limited, be kept: goyng alwayes, perpendicularly, vnder the way, on earth designed: And, contrarywise, Any way, (straight or croked,) vnder the earth, beyng giuen: vppon the vtface, or Superficies of the earth, to Lyne out the same: So, as, from the Centre of the earth, perpendiculars drawn to the Sphæricall Superficies of the earth, shall precisely fall in the Correspondent pointes of those two wayes. This, with all other Cases and circumstances herein, and appertenances, this Arte demonstrateth. This Arte, is very ample in varietie of Conclusions: and very profitable sundry wayes to the Common Wealth. The occasion of my Inuenting this Arte, was at the request of two Gentlemen, who had a certaine worke (of gaine) vnder

ground: and their groundes did ioyn euer the worke: and by reason of the crookednes, diuers depthes, and heithes of the way vnder ground, they were in doubt, and at controuersie, vnder whose ground, as then, the worke was. The name onely (before this) was of me published, *De Itinere Subterraneo*: The rest, be at Gods will. For Pioners, Miners, Diggers for Mettalls, Stone, Cole, and for secrete passages vnder ground, betwene place and place (as this land hath diuerse) and for other purposes, any man may easily perceau, both the great fruite of this Arte, and also in this Arte, the great aide of Geometrie.

Hydragogie, demonstrateth the possible leading of Water, by Natures lawe, and by artificiall helpe, from any head (being a Spring, standing, or running Water) to any other place assigned. Long, hath this Arte bene in vse: and much thereof written: and very marueilous workes therein, performed: as may yet appeare, in Italy: by the Ruynes remaining of the Aqueductes. In other places, of Riuers leading through the Maine land, Nauigable many a Mile. And in other places, of the marueilous forcings of Water to Ascend. which all, declare the great skill, to be required of him, who should in this Arte be perfecte, for all occasions of waters possible leading. To speake of the allowance of the Fall, for euery hundred foote: or of the Ventills (if the waters labour be farre, and great) I neede not: Seing, at hand (about vs) many expert men can sufficiently testifie, in effecte, the order: though the Demonstration of the Necessitie thereof, they know not: Nor yet, if they should be led, vp and downe, and about Mountaines, from the head of the Spring: and then, a place being assigned: and of them, to be demaunded, how low or high, that last place is, in respecte of the head, from which (so crookedly, and vp and downe) they be come: Perhaps, they would not, or could not, very redily, or nerely assoyle that question. *Geometrie* therefore, is necessary to *Hydragogie*. Of the sundry wayes to force water to ascend, eyther by *Tympane*, *Kettell mills*, *Skrue*, *Ctesibike*, or such like: in *Vitruuius*, *Agricola*, (and

other,) fully, the maner may appeare. And so, thereby, also be most euident, how the Artes, of *Pneumatithmie*, *Helicosophie*, *Statike*, *Trochilike*, and *Menadrie*, come to the furniture of this, in Speculation, and to the Commoditie of the Common Wealth, in practise.

Horometrie, is an Arte Mathematicall, which demonstrateth, how, at all times appointed, the precise vsuall denominatiõ of time, may be knowen, for any place assigned. These wordes, are smoth and plaine easie Englishe, but the reach of their meaning, is farther, then you woulde lightly imagine. Some part of this Arte, was called in olde time, *Gnomonice*: and of late, *Horologiographia*: and in Englishe, may be termed, *Dialling*. Auncient is the vse, and more auncient, is the Inuention. The vse, doth well appeare to haue bene (at the least) aboue two thousand and three hundred yeare agoe: in* 4. Reg. Diall, then, by the Sunne, shewing the distinction of time. By Sunne, Mone, and Sterres, this Dialling may be performed, and the precise Time of day or night knowen. But the demonstratiue delineation of these Dialls, of all sortes, requireth good skill, both of *Astronomie*, and *Geometrie* Elementall, Sphæricall, Phænomenall, and Conikall. Then, to vse the groundes of the Arte, for any regular Superficies, in any place offred: and (in any possible apt position therof) thereon, to describe (all maner of wayes) how, vsuall howers, may be (by the *Sunnes* shadow) truly determined: will be found no sleight Painters worke. So to Paint, and prescribe the Sunnes Motion, to the breadth of a heare. In this Feate (in my youth) I Inuented a way, How in any Horizontall, Murall, or Æquinociall Diall, &c. At all howers (the Sunne shining) the Signe and Degree ascendent, may be knowen. Which is a thing very necessary for the Rising of those fixed Sterres: whose Operation in the Ayre, is of great might, euidently. I speake no further, of the vse hereof. Bur forasmuch as, Mans affaires require knowledge of Times & Momentes, when, neither Sunne, Mone, or Sterre, can be sene: Therefore, by Industrie

Mechanicall, was inuented, first, how, by Water, running orderly, the Time and howers might be knowen: whereof, the famous *Ctesibius*, was Inuentor: a man, of *Vitruuius*, to the Skie (iustly) extolled. Then, after that, by Sand running, were howers measured: Then, by *Trochilike* with waight: And of late time, by *Trochilike* with Spring: without waight. All these, by Sunne or Sterres direction (in certaine time) require ouersight and reformation, according to the heauenly *Æquinoctiall* Motion: besides the inæqualitie of their owne Operation. There remayneth (without parabolically meaning herein) among the Philosophers,

~~A peritrochilike Motion~~ *A peritrochilike Motion*, more commodious, and more marueilous way, then all these: of hauing the motion of the Primouant (or first æquinoctiall motion,) by Nature and Arte, Imitated: which you shall (by further search in waightier studyes) hereafter, vnderstand more of. And so, it is tyme to finish this Annotation, of Tymes distinction, vsed in our common, and priuate affaires: The commoditie wherof, no man would want, that can tell, how to bestow his tyme.

Zographie, is an Arte Mathematicall, which teacheth and demonstrateth, how, the Intersection of all visuall Pyramides, made by any playne assigned, (the Centre, distance, and lightes, beyng determined) may be, by lynes, and due propre colours, represented. A notable Arte, is this: and would require a whole Volume, to declare the property thereof: and the Commodities ensuyng. Great skill of *Geometrie*, *Arithmetike*, *Perspectiue*, and *Anthropographie*, with many other particular Artes, hath the *Zographer*, nede of, for his perfection. For, the most excellent Painter, (who is but the propre Mechanicien, & Imitator sensible, of the Zographer) hath attained to such perfection, that Sense of Man and beast, haue iudged thinges painted, to be things naturall, and not artificiall: aliue, and not dead. This Mechanicall Zographer (commonly called the Painter) is meruailous in his skill: and seemeth to haue a certaine diuine power: As, of frendes absent, to make a frendly, present comfort: yea, and of frendes dead, to giue a continuall, silent presence: not onely with vs, but with our posteritie, for many Ages. And so procedyng, Consider, How, in Winter, he can shew you, the liuely vew of Sommers Ioy, and riches: and in Sommer, exhibite the countenance of Winters dolefull State, and nakednes. Cities, Townes, Fortes, Woodes, Armyes, yea whole Kingdomes (be they neuer so farre, or greate) can he, with ease, bring with him, home (to any mans Iudgement) as Paternes liuely, of the thinges rehearsed. In one little house, can he, enclose (with great pleasure of the beholders,) the portrayture liuely, of all visible Creatures, either on earth, or in the earth, liuing: or in the waters lying, Creping, slyding, or swimming: or of any foule, or fly, in the ayre flying. Nay, in respect of the Starres, the Skie, the Cloudes: yea, in the shew of the very light it selfe (that Diuine Creature) can he match our eyes Iudgement, most nerely. What a thing is this? thinges not yet being, he can represent so, as, at their being, the

Picture shall seame (in maner) to haue Created them. To what Artificer, is not Picture, a great pleasure and Commoditie? Which of them all, will refuse the Direction and ayde of Picture? The Architect, the Goldsmith, and the Arras Weauer: of Picture, make great account. Our liuely Herbals, our portraitures of birdes, beastes, and fishes: and our curious Anatomies, which way, are they most perfectly made, or with most pleasure, of vs beholden? Is it not, by Picture onely? And if Picture, by the Industry of the Painter, be thus commodious and meruailous: what shall be thought of *Zographie*, the Scholemaster of Picture, and chief gouernor? Though I mencion not *Sculpture*, in my Table of Artes Mathematicall: yet may all men perceiue, How, that *Picture* and *Sculpture*, are Sisters germaine: and both, right profitable, in a Commõ wealth. and of *Sculpture*, aswell as of Picture, excellent Artificers haue written great bokes in commendation. Witnesse I take, of *Georgio Vasari*, *Pittore Aretino*: of *Pomponius Gauricus*: and other. To these two Artes, (with other,) is a certaine od Arte, called *Althalmasat*, much beholding: more, then the common *Sculptor*, *Entayler*, *Keruer*, *Cutter*, *Grauer*, *Founder*, or *Paynter* (&c) know their Arte, to be commodious.

~~Architecture~~ **Architecture**, to many may seme not worthy, or not mete, to be reckned among the *Artes Mathematicall*. To whom, I thinke good, to giue some account of my so doying. Not worthy, (will they say,) bycause it is but for building, of a house, Pallace, Church, Forte, or such like, grosse workes. And you, also, defined the *Artes Mathematicall*, to be such, as dealt with no Materiall or corruptible thing: and also did demonstratiuely procede in their faculty, by Number or Magnitude. First you ~~The Architect~~ *The Architect* account, here, *Architecture*, among those *Artes Mathematicall*, which are Deriued from the Principals: and you know, that such, may deale with Naturall thinges, and sensible matter. Of which, some draw nerer, to the Simple and absolute Mathematicall Speculation, then other. And though, the *Architect* procureth, enformeth, & directeth, the *Mechanicien*, to handworke, & the building actuall, of house,

Castell, or Pallace, and is chief Iudge of the same: yet, with him
 selfe (as chief *Master* and *Architect*,) remaineth the Demonstratiue
 reason and cause, of the Mechaniciens worke: in Lyne, plaine, and
 Solid: by *Geometricall*, *Arithmetically*, *Opticall*, *Musically*,
Astronomicall, *Cosmographicall* (& to be brief) by all the former
 Deriued *Artes Mathematicall*, and other Naturall Artes, hable to be
 confirmed and stablished. If this be so: then, may you thinke, that
Architecture, hath good and due allowance, in this honest
 Company of *Artes Mathematicall* Deriuatiue. I will, herein, craue
 Iudgement of two most perfect *Architectes*: the one, being
Vitruuius, the Romaine: who did write ten bookes thereof, to the
 Emperour *Augustus* (in whose daies our Heauenly Archemaster,
 was borne): and the other, *Leo Baptista Albertus*, a Florentine:
 who also published ten bookes therof. *Architectura* (sayth
Vitruuius) *est Scientia pluribus disciplinis & varijs eruditionibus*
ornata: cuius Iudicio probantur omnia, quæ ab cæteris Artificibus
perficiuntur opera. That is. *Architecture*, is a Science
 garnished with many doctrines & diuerse instructions: by
 whose Iudgement, all workes, by other workmen finished,
 are Iudged. It followeth. *Ea nascitur ex Fabrica, &*
Ratiocinatione. &c. Ratiocinatio autem est, quæ, res fabricatas,
Solertia ac ratione proportionis, demonstrare atq^{ue} explicare
potest. Architecture, groweth of Framing, and Reasoning.
&c. Reasoning, is that, which of thinges framed, with
forecast, and proportion: can make demonstration, and
manifest declaration. Againe. *Cùm, in omnibus enim rebus, tùm*
maximè etiam in Architectura, hæc duo insunt: quod significatur,
& quod significat. Significatur proposita res, de qua dicitur: hanc
autem Significat Demonstratio, rationibus doctrinarum explicata.
Forasmuch as, in all thinges: therefore chiefly in
Architecture, these two thinges are: the thing signified: and
that which signifieth. The thing propounded, whereof we
speake, is the thing Signified. But Demonstration,
expressed with the reasons of diuerse doctrines, doth

signifie the same thing. After that. Vt literatus sit, peritus Graphidos, eruditus Geometriæ, & Optices non ignarus: instructus Arithmetica: historias complures nouerit, Philosophos diligenter audiuerit: Musicam sciuerit: Medicinæ non sit ignarus, responsa Iurisperitorũ nouerit: Astrologiam, Cæliq^{ue} rationes cognitatas habeat. An Architect (sayth he) ought to vnderstand Languages, to be skilfull of Painting, well instructed in Geometrie, not ignorant of Perspectiue, furnished with Arithmetike, haue knowledge of many histories, and diligently haue heard Philosophers, haue skill of Musike, not ignorant of Physike, know the aunsweres of Lawyers, and haue Astronomie, and the courses Cælestiall, in good knowledge. He geueth reason, orderly, wherefore all these Artes, Doctrines, and Instructions, are requisite in an excellent Architect. And (for breuitie) omitting the Latin text, thus he hath. Secondly, it is behofefull for an Architect to haue the knowledge of Painting: that he may the more easilie fashion out, in patternes painted, the forme of what worke he liketh. And Geometrie, geueth to Architecture many helpes: and first teacheth the Vse of the Rule, and the Cumpasse: wherby (chiefly and easilie) the descriptions of Buildinges, are despatched in Groundplats: and the directions of Squires, Leuells, and Lines. Likewise, by Perspectiue, the Lightes of the heauen, are well led, in the buildinges: from certaine quarters of the world. By Arithmetike, the charges of Buildinges are summed together: the measures are expressed, and the hard questions of Symmetries, are by Geometricall Meanes and Methods discoursed on. &c. Besides this, of the Nature of thinges (which in Greke is called φυσιολογία) Philosophie doth make declaration. Which, it is necessary, for an Architect, with diligence to haue learned: because it hath many and diuers naturall questions: as specially, in Aqueductes. For in their courses,

leadinges about, in the leuell ground, and in the mountinges, the naturall Spirites or breathes are ingendred diuers wayes: The hindrances, which they cause, no man can helpe, but he, which out of Philosophie, hath learned the originall causes of thinges. Likewise, who soeuer shall read Ctesibius, or Archimedes bookes, (and of others, who haue written such Rules) can not thinke, as they do: vnlesse he shall haue receaued of Philosophers, instructions in these thinges. And Musike he must nedes know: that he may haue vnderstanding, both of Regular and Mathematicall Musike: that he may temper well his Balistes, Catapultes, and Scorpions. &c. Moreouer, the Brasen Vessels, which in Theatres, are placed by Mathematicall order, in ambries, vnder the steppes: and the diuersities of the soundes (which y^e Grecians call ἡμεῖς) are ordred according to Musicall Symphonies & Harmonies: being distributed in y^e Circuities, by Diatessaron, Diapente, and Diapason. That the conuenient voyce, of the players sound, whẽ it came to these preparations, made in order, there being increased: with y^t increasing, might come more cleare & pleasant, to y^e eares of the lokers on. &c. And of Astronomie, is knowẽ y^e East, West, South, and North. The fashion of the heauen, the Æquinox, the Solsticie, and the course of the sterres. Which thinges, vnleast one know: he can not perceiue, any thyng at all, the reason of Horologies. Seyng therfore this ample Science, is garnished, beautified and stored, with so many and sundry skils and knowledges: I thinke, that none can iustly account them selues Architectes, of the suddeyne. But they onely, who from their childes yeares, ascendyng by these degrees of knowledges, beyng fostered vp with the atteynyng of many Languages and Artes, haue wonne to the

high Tabernacle of Architecture. &c. And to whom Nature hath giuen such quicke Circumspection, sharpnes of witt, and Memorie, that they may be very absolutely skillfull in Geometrie, Astronomie, Musike, and the rest of the Artes Mathematicall: Such, surmount and passe the callyng, and state, of Architectes: ~~And thus become~~ Mathematiciens. &c. And they are found, seldome. As, in tymes past, was Aristarchus Samius: Philolaus, and Archytas, Tarentynes: Apollonius Pergæus: Eratosthenes Cyreneus: Archimedes, and Scopas, Syracusians. Who also, left to theyr posteritie, many Engines and Gnomonicall workes: by numbers and naturall meanes, inuented and declared.

Thus much, and the same wordes (in sense) in one onely Chapter of this Incōparable Architect Vitruuius, shall you finde. And if you should, but take his booke in your hand, and slightly loke thorough it, you would say straight wth ~~This is~~ ~~Geometrye~~, Arithmetike, Astronomie, Musike, Anthropographie, Hydragogie, Horometrie. &c. and (to cōclude) the Storehouse of all workmāship. Now, let vs listen to our other Iudge, our Florentine, *Leo Baptista*: and narrowly consider, how he doth determine of Architecture. *Sed anteq^{ue} vltra progrediar.* &c. But before I procede any further (sayth he) I thinke, that I ought to expresse, what man I would haue to bee allowed an Architect. For, I will not bryng in place a Carpenter: as though you might Compare him to the Chief Masters of other Artes. For the hand of the Carpenter, is the Architectes Instrument. VWho is an Architect? I will appoint the Architect to be that man, who hath the skill, (by a certaine and meruailous meanes and way,) both in minde and Imagination to determine and also in worke to finish: what workes so euer, by motion of waight, and cuppling and framying together of bodyes, may most aptly be Commodious for the worthiest Vses of Mañ. And that he

may be able to performe these thinges, he hath nede of
 attenyng and knowledge of the best, and most worthy
 thynges. &c. The whole Feate of Architecture in buildyng,
 consisteth in Lineamentes, and in Framyng. And the whole
 power and skill of Lineamentes, tendeth to this: that the
 right and absolute way may be had, of Coaptyng and
 ioyning Lines and angles: by which, the face of the
 buildyng or frame, may be comprehended and concluded.
 And it is the property of Lineamentes, to prescribe vnto
 buildynges, and euery part of them, an apt place, &
 certaine nũber: a worthy maner, and a semely order: that,
 so, y^e whole forme and figure of the buildyng, may rest in
 the very Lineamentes. &c. And we may prescribe in mynde
 and imagination the whole formes, * * The Immaterialitie of
 perfect ~~Architecturall~~ stuffe beyng secluded. Which point we
 shall attayne, by Notyng and forepointyng the angles, and
 lines, by a sure and certaine direction and connexion.
 Seyng then, these thinges, are thus: ~~Whdt is Lineamenta~~, is.
 shalbe the certaine and constant prescribyng, conceiued in
 mynde: made in lines and angles: and finished with a
 learned minde and wyt. We thanke you Master Baptist, that you
 haue so aptly brought your Arte, and phrase therof, to haue some
 Mathematicall perfectione. ~~By this~~ Note, nũber, forme, figure, and
 Symmetrie mentall: all naturall & sensible stuffe set a part. Now,
 then, it is euident, (Gentle reader) how aptely and worthely, I haue
 preferred *Architecture*, to be bred and fostered vp in the Dominion
 of the pereles *Princesse, Mathematica*: and to be a naturall Subject
 of hers. And the name of *Architecture*, is of the principalitie, which
 this Science hath, aboue all other Artes. And *Plato* affirmeth, the
Architect to be *Master* ouer all, that make any worke. Wherupon,
 he is neither Smith, nor Builder: nor, separately, any Artificer: but
 the Hed, the Prouost, the Directer, and Iudge of all Artificiall
 workes, and all Artificers. For, the true *Architect*, is hable to teach,

Demonstrate, distribute, describe, and Iudge all workes wrought. And he, onely, searcheth out the causes and reasons of all Artificiall thynges. Thus excellent, is *Architecture*: though few (in our dayes) attayne thereto: yet may not the Arte, be otherwise thought on, then in very dede it is worthy. Nor we may not, of auncient Artes, make new and imperfect Definitions in our dayes: for scarsitie of Artificers: No more, than we may pynche in, the Definitions of *Wisedome*, or *Honestie*, or of *Frendeshyp* or of *Iustice*. No more will I consent, to Diminish any whit, of the perfection and dignitie, (by iust cause) allowed to absolute *Architecture*. Vnder the Direction of this Arte, are thre principall, necessary *Mechanicall Artes*. Namely, *Howsing*, *Fortification*, and *Naupegie*. *Howsing*, I vnderstand, both for Diuine Seruice, and Mans common vsage: publike, and priuate. Of *Fortification* and *Naupegie*, straunge matter might be told you: But perchaunce, some will be tyred, with this Bederoll, all ready rehearsed: and other some, will nycely nip my grosse and homely discoursing with you: made in post hast: for feare you should wante this true and frendly warnyng, and tast giuyng, of the *Power Mathematicall*. Lyfe is short, and vncertaine: Tymes are perillouse: &c. And still the Printer awayting, for my pen staying: All these thinges, with farder matter of Ingratefulnes, giue me occasion to passe away, to the other Artes remainyng, with all spede possible.

THE Arte of Nauigation, demonstrateth how, by the shortest good way, by the aptest Directiõ, & in the shortest time, a sufficient Ship, betwene any two places (in passage Nauigable,) assigned: may be cõducted: and in all stormes, & naturall disturbances chauncyng, how, to vse the best possible meanes, whereby to recouer the place first assigned. What nede, the *Master Pilote*, hath of other Artes, here before recited, it is easie to know: as, of *Hydrographie*, *Astronomie*, *Astrologie*, and *Horometrie*. Presupposing continually, the common Base, and foundation of all: namely *Arithmetike* and *Geometrie*. So that, he be hable to vnderstand, and Iudge his own

necessary Instrumentes, and furniture Necessary: Whether they be perfectly made or no: and also can, (if nede be) make them, hym selfe. As Quadrantes, The Astronomers Ryng, The Astronomers staffe, The Astrolabe vniuersall. An Hydrographicall Globe. Charts Hydrographicall, true, (not with parallell Meridians). The Common Sea Compas: The Compas of variacion: The Proportionall, and Paradoxall Compasse(of man inuented), for our two Moscouy Master Pilotes, at the request of the Company) Clockes with spryng: houre, halfe houre, and three houre Sandglasses: & sundry other Instrumētes: And also, be hable, on Globe, or Playne to describe the Paradoxall Compasse: and duely to vse the same, to all maner of purposes, whereto it was inuented. And also, be hable to Calculate the Planetes places for all tymes.

Moreouer, with Sonne Mone or Sterre (or without) be hable to define the Longitude & Latitude of the place, which he is in: So that, the Longitude & Latitude of the place, from which he sayled, be giuen: or by him, be knowne. whereto, appertayneth expert meanes, to be certified euer, of the Ships way. &c. And by foreseing the Rising, Settyng, Nonestedyng, or Midnightyng of certaine tempestuous fixed Sterres: or their Coniunctions, and Anglynges with the Planetes, &c. he ought to haue expert coniecture of Stormes, Tempestes, and Spoutes: and such lyke Meteorologicall effectes, daungerous on Sea. For (as *Plato* sayth,)

Mutationes, opportunitatesq^{ue} temporum presentire, non minus rei militari, quàm Agriculturæ, Nauigationiq^{ue} conuenit. To foresee the alterations and opportunities of tymes, is conuenient, no lesse to the Art of Warre, then to Husbandry and Nauigation. And besides such cunnyng meanes, more eident tokens in Sonne and Mone, ought of hym to be knowen: such as (the Philosophicall Poëte) *Virgilius* teacheth, in hys *Georgikes*. Where he sayth, C

*Sol quoq^{ue} & exoriens & quum se condet in vndas,
Signa dabit, Solem certissima signa sequuntur. &c.
Georgic. 1.*

————— *Nam sæpe videmus,*
Ipsius in vultu varios errare colores.
Cæruleus, pluuiam denunciat, igneus Euros.
Sin maculæ incipient rutilo immiscerier igni,
Omnia tum pariter vento, nimbisq^{ue} videbis
Feruere: non illa quisquam me nocte per altum
Ire, neq^{ue} a terra moueat conuellere funem. &c.
Sol tibi signa dabit. Solem quis dicere falsum
Audeat? ————— &c.

And so of Mone, Sterres, Water, Ayre, Fire, Wood, Stones, Birdes, and Beastes, and of many thynges els, a certaine Sympathicall forewarnyng may be had: sometymes to great pleasure and proffit, both on Sea and Land. Sufficently, for my present purpose, it doth appeare, by the premisses, how *Mathematicall*, the *Arte* of *Nauigation*, is: and how it nedeth and also vseth other *Mathematicall Artes*: And now, if I would go about to speake of the manifold Commodities, commyng to this Land, and others, by Shypps and *Nauigation*, you might thinke, that I catch at occasions, to vse many wordes, where no nede is.

Yet, this one thyng may I, (iustly) say. In *Nauigation*, none ought to haue greater care, to be skillfull, then our English Pylotes. And perchaunce, Some, would more attempt: And other Some, more willingly would be aydyng, it they wist certainly, What Priuiledge, God had endued this Iland with, by reason of Situation, most commodious for *Nauigation*, to Places most Famous & Riche. And though, * *Annals* (off 1567) *Hy Gung* Gentleman, a Courragious Capitaine, was in a great readynes, with good hope, and great causes of persuasion, to haue ventured, for a Discouerye, (either *Westerly*, by *Cape de Paramantia*: or *Esterly*, aboue *Noua Zemla*, and the *Cyremisses*) and was, at the very nere tyme of Attemptyng, called and employed otherwise (both then, and since,) in great good seruice to his Countrey, as the Irish Rebels haue *tasted: Yet, *Asmy* (1569) (though the same Gentleman, doo not hereafter, deale therewith) Some one, or other, should listen to the Matter:

and by good aduise, and discrete Circumspection, by little, and little, wyne to the sufficient knowledge of that Trade and Voyage: Which, now, I would be sory, (through Carelesnesse, want of Skill, and Courrage,) should remayne Vnknowne and vnheard of. Seyng, also, we are herein, halfe Challenged, by the learned, by halfe request, published. Therof, verely, might grow Commoditye, to this Land chiefly, and to the rest of the Christen Common wealth, farre passing all riches and worldly Threasure.

Thaumaturgike, is that Art Mathematicall, which giueth certaine order to make straunge workes, of the sense to be perceiued, and of men greatly to be wondred at. By sundry meanes, this *Wonder-work* is wrought. Some, by *Pneumatithmie*. As the workes of *Ctesibius* and *Hero*, Some by waight. wherof *Timæus* speaketh. Some, by Stringes strayned, or Springs, therwith Imitating liuely Motions. Some, by other meanes, as the Images of Mercurie: and the brasen hed, made by *Albertus Magnus*, which dyd seme to speake. *Boethius* was excellent in these feates. To whom, *Cassiodorus* writyng, sayth. *Your purpose is to know profound thynges: and to shew meruayles. By the disposition of your Arte, Metals do low: Diomedes of brasse, doth blow a Trumpet loude: a brasen Serpent hisseth: byrdes made, sing swetely. Small thynges we rehearse of you, who can Imitate the heauen. &c.* Of the straunge Selfmouyng, which, at Saint Denys, by Paris, * *Anno. 1551* *et 1552* *twise* (*Orontius* beyng then with me, in Company) it were to straunge to tell. But some haue written it. And yet, (I hope) it is there, of other to be sene. And by *Perspectiue* also straunge thinges, are done. As partly (before) I gaue you to vnderstand in *Perspectiue*. As, to see in the Ayre, a loft, the lyuely Image of an other man, either walkyng to and fro: or standyng still. Likewise, to come into an house, and there to see the liuely shew of Gold, Siluer or precious stones: and commyng to take them in your hand, to finde nought but Ayre. Hereby, haue some men (in all other matters counted wise) foully ouershot thẽ selues: misdeaming of

the meanes. Therefore sayd *Claudius Cælestinus*. *De his quæ*
Mundo mirabiliter hodiæ magnæ & literaturæ viros & magna
reputationis videmus, opera quedam quasi miranda, supra Naturã
putare: de quibus in Perspectiua doctus causam faciliter
reddidisset. That is. Now a dayes, we see some men, yea of
 great learnyng and reputation, to Iudge certain workes as
 meruaylous, aboue the power of Nature: Of which workes,
 one that were skillfull in Perspectiue might easely haue
 giuen the Cause. Of *Archimedes Sphære*, *Cicero* witnesseth.
 It is very straunge to thinke on. For when *Archimedes* (sayth he)
 did fasten in a Sphære, the mouynges of the Sonne, Mone,
 and of the fiue other Planets, he did, as the God, which (in
Timæus of *Plato*) did make the world. That, one turnyng,
 should rule motions most vnlike in slownes, and swiftnes.
 But a greater cause of meruayling we haue by *Claudianus* report
 hereof. Who affirmeth this *Archimedes worke*, to haue ben of
 Glasse. And discourseth of it more at large: which I omit. The
 Doue of wood, which the *Mathematicien Archytas* did make to
 flye, is by *Agellius* spoken of. Of *Dædalus* straunge Images, *Plato*
 leaueth in writyng. *Aristotle*, in hys *Politikes*, of both, maketh
 mention. Meruaylous was the workemanshyp, of late dayes,
 performed by good skill of *Trochilike*. &c. For in *Noremburge*,
 A flye of Iern, beyng let out of the Artificers hand, did (as it were)
 fly about by the gestes, at the table, and at length, as though it
 were weary, retourne to his masters hand agayne. Moreouer, an
 Artificiall Egle, was ordred, to fly out of the same Towne,
 a mighty way, and that a loft in the Ayre, toward the Emperour
 comming thether: and followed hym, beyng come to the gate of
 the towne. Thus, you see, what, *Arte Mathematicall* can performe,
 when Skill, will, Industry, and Hability, are duely applyed to profe.
 And *Diogenes*, and such like marueilous Actes and Feates,
 Naturally, Mathematically, and Mechanically, wrought and
 contriued: ouer the longest Student, and Modest Christian

Philosopher, be counted, & called a Coniurer? Shall the folly of Idiotes, and the Mallice of the Scornfull, so much preuaile, that He, who seeketh no worldly gaine or glory at their handes: But onely, of God, the threasor of heauenly wisdom, & knowledge of pure veritie: Shall he (I say) in the meane space, be robbed and spoiled of his honest name and fame? He that seketh (by S. Paules aduertisement) in the Creatures Properties, and wonderfull vertues, to finde iuste cause, to glorifie the Æternall, and Almighty Creator by: Shall that man, be (in hugger mugger) condemned, as a Companion of the Helhoundes, and a Caller, and Coniurer of wicked and damned Spirites? He that bewaileth his great want of time, sufficient (to his contentation) for learning of Godly wisdom, and Godly Verities in: and onely therin setteth all his delight: Will that mā leese and abuse his time, in dealing with the Chiefe enemy of Christ our Redemer: the deadly foe of all mankind: the subtile and impudent peruerter of Godly Veritie: the Hypocriticall Crocodile: the Enuious Basiliske, continually desirous, in the twinke of an eye, to destroy all Mankind, both in Body and Soule, æternally? Surely (for my part, somewhat to say herein) I haue not learned to make so brutish, and so wicked a Bargaine. Should I, for my xx. or xxv. yeares Studie: for two or three thousand Markes spending: seuen or eight thousand Miles going and trauailing, onely for good learninges sake: And that, in all maner of wethers: in all maner of waies and passages: both early and late: in daunger of violence by man: in daunger of destruction by wilde beastes: in hunger: in thirst: in perillous heates by day, with toyle on foote: in daungerous dampes of colde, by night, almost bereuing life: (as God knoweth): with lodgings, oft times, to small ease: and sometime to lesse securitie. And for much more (then all this) done & suffred, for Learning and attaining of Wisdom: Should I (I pray you) for all this, no otherwise, nor more warily: or (by Gods mercifulnes) no more luckily, haue fished, with so large, and costly, a Nette, so long time in drawing (and that with the helpe and aduise of Lady Philosophie, & Queene Theologie): but at length, to haue catched, and drawn

vp,* * *A prouerb. Fayre fisht, and Enought Na Frye, as Deuill?* For, so,
doth the Common peuish Pratler Imagine and Iangle: And, so, doth
the Malicious skorner, secretly wishe, & brauely and boldly face
down, behinde my backe. Ah, what a miserable thing, is this kinde
of Men? How great is the blindnes & boldnes, of the Multitude, in
thinges about their Capacitie? What a Land: what a People: what
Maners: what Times are these? Are they become Deuils, them
selues: and, by false witsnesse bearing against their Neighbour,
would they also, become Murderers? Doth God, so long geue them
respice, to reclaime them selues in, from this horrible slaundering
of the giltlesse: contrary to their owne Consciences: and yet will
they not cease? Doth the Innocent, forbear the calling of them,
Iuridically to aunswere him, according to the rigour of the Lawes:
and will they despise his Charitable pacience? As they, against
him, by name, do forge, fable, rage, and raise slaunder, by Worde
& Print: Will they prouoke him, by worde and Print, likewise, to
Note their Names to the World: with their particular deuises,
fables, beastly Imaginations, and vnchristen-like slaunders? Well:
Well. O (you such) my vnkinde Countrey men. O vnnaturall
Countrey men. O vnthankfull Countrey men. O Brainsicke, Rashe,
Spitefull, and Disdainfull Countrey men. Why oppresse you me,
thus violently, with your slaundering of me: Contrary to Veritie:
and contrary to your owne Consciences? And I, to this hower,
neither by worde, deede, or thought, haue bene, any way, hurtfull,
damageable, or iniurious to you, or yours? Haue I, so long, so
dearly, so farre, so carefully, so painfully, so daungerously sought
& trauailed for the learning of Wisedome, & atteyning of Vertue:
And in the end (in your iudgemēt) am I become, worse, then when
I begā? Worse, thē a Mad man? A dangerous Member in the
Common Wealth: and no Member of the Church of Christ? Call
you this, to be Learned? Call you this, to be a Philosopher? and a
louer of Wisedome? To forsake the straight heauenly way: and to
wallow in the broad way of damnation? To forsake the light of
heauenly Wisedome: and to lurke in the dungeon of the Prince of
darkenesse? To forsake the Veritie of God, & his Creatures: and to
fawne vpon the Impudent, Craftie, Obstinate Lier, and continuall

disgracer of Gods Veritie, to the vttermost of his power? To forsake the Life & Blisse Æternall: and to cleaue vnto the Author of Death euerlasting? that Murderous Tyrant, most greedily awaiting the Pray of Mans Soule? Well: I thanke God and our Lorde Iesus Christ, for the Comfort which I haue by the Examples of other men, before my time: To whom, neither in godlines of life, nor in perfection of learning, I am worthy to be compared: and yet, they sustained the very like Iniuries, that I do: or rather, greater. Pacient *Socrates*, his *Apologie* will testifie: *Apuleius* his *Apologies*, will declare the Brutishnesse of the Multitude. *Ioannes Picus*, Earle of Mirandula, his *Apologie* will teach you, of the Raging slaunder of the Malicious Ignorant against him. *Ioannes Trithemius*, his *Apologie* will specifie, how he had occasion to make publike Protestation: as well by reason of the Rude Simple: as also, in respect of such, as were counted to be of the wisest sort of men. Many could I recite: But I deferre the precise and determined handling of this matter: being loth to detect the Folly & Mallice of my Natiue Countrey men. Who, so hardly, can digest or like any extraordinary course of Philosophicall Studies: not falling within the Cumpasse of their Capacitie: or where they are not made priuie of the true and secrete cause, of such wonderfull Philosophicall Feates. These men, are of fower sortes, chiefly. The first, I may name, *Vaine pratling busie bodies*: The second, *Fond Frenedes*: The third, *Imperfectly zelous*: and the fourth, *Malicious Ignorant*. To eche of these (briefly, and in charitie) I will say a word or two, and so returne to my Preface. *Vaine pratling busie bodies*, vse your idle assemblies, and conferences, otherwise, then in talke of matter, either aboue your Capacities, for hardnesse: or contrary to your Consciences. *Fond Frenedes*, leaue of, so to commend your vnacquainted frend, vpon blinde affection: As, because he knoweth more, then the common Student: that, therefore, he must needes be skilfull, and a doer, in such matter and maner, as you terme *Coniuring*. Weening, thereby, you aduaunce his fame: and that you make other men, great marueilers of your hap, to haue such a learned frend. Cease to ascribe Impietie, where you pretend

Amitie. For, if your tounge were true, then were that your frend,
Vntrue, both to God, and his Soueraigne. Such *Frendes* and
Fondlinges, I shake of, and renounce you: Shake you of, your
Folly zealous, to you, do I say: that (perhaps) well, do you Meane:
 But farre you misse the Marke: If a Lambe you will kill, to feede
 the flocke with his bloud. Sheepe, with Lambes bloud, haue no
 naturall sustenance: No more, is Christes flocke, with horrible
 slaunders, duely ædified. Nor your faire pretense, by such rashe
 ragged Rhetorike, any whit, well graced. But such, as so vse me,
 will finde a fowle Cracke in their Credite. Speake that you know:
 And know, as you ought: Know not, by Heare say, when life lieth
 in daunger. Search to the quicke, & let Charitie be *Multigarde*. 4.
Ignorant, what shall I say to thee? *Prohibe linguam tuam a malo.*
A detractiōe parcite linguæ. Cause thy tounge to refraine frō
euill. Refraine your tounge from slaunder. Though your
 tounge be sharpned, Serpent like, & Adders poyson lye in your
 lippes, take heed, and thinke, betimes, with your selfe, *Vir*
linguosus non stabilietur in terra. Virum violentum venabitur
malum, donec præcipitetur. For, sure I am, *Quia faciet Dominus*
Iudicium afflicti: & vindictam pauperum.

Thus, I require you, my assured frendes, and Countrey men (you
 Mathematiciens, Mechaniciens, and Philosophers, Charitable and
 discrete) to deale in my behalf, with the light & vntrue tounge,
 my enuious Aduersaries, or Fond frends. And farther, I would
 wishe, that at leysor, you would consider, how *Basilius Magnus*,
 layeth *Moses* and *Daniel*, before the eyes of those, which count all
 such Studies Philosophicall (as mine hath bene) to be vngodly, or
 vnprofitable. Waye well *S. Stephen* his witnesse of *Moses*. *Act.*
s7 Moses omni Sapientia Ægyptiorũ: & erat potens in verbis &
operibus suis. Moses was instructed in all maner of
wisedome of the Ægyptians: and he was of power both in
his wordes, and workes. You see this Philosophicall Power &
 Wisedome, which *Moses* had, to be nothing misliked of the Holy
 Ghost. Yet *Plinius* hath recorded, *Moses* to be a wicked *Magicien*.
 And that (of force) must be, either for this Philosophicall

wisedome, learned, before his calling to the leading of the Children of *Israel*: or for those his wonders, wrought before King *Pharao*, after he had the conducting of the *Israelites*. As concerning the first, you perceave, how *S. Stephen*, at his Martyrdome (being full of the Holy Ghost) in his Recapitulation of the olde Testament, hath made mention of *Moses Philosophie*: with good liking of it: And *Basilius Magnus* also, auoucheth it, to haue bene to *Moses* profitable (and therefore, I say, to the Church of God, necessary). But as cōcerning *Moses* wonders, done before King *Pharao*: God, him selfe, sayd: *Vide vt omnia ostenta, quæ posui in manu tua, facias coram Pharaone. See that thou do all those wonders before Pharao, which I haue put in thy hand.* Thus, you euidently perceave, how rashly, *Plinius* hath slaundered *Moses*, ~~of his~~ ^{of his} ~~Magike~~ ^{Magike}, saying: *Est & alia Magices Factio, a Mose, Iamne, & Iotape, Iudæis pendens: sed multis millibus annorum post Zorodastan.* ~~Israel such,~~ therefore, who, in Iudgement and Skill of Philosophie, are farre Inferior to *Plinie*, take good heede, least they ouershoot them selues rashly, in giuing of *Philosophers straunge Actes*: and the Meanes, how they are ~~more~~ ^{more}, ought they to beware of forging, deuising, and imagining monstrous feates, and wonderfull workes, when and where, no such were done: no, not any sparke or likelihode, of such, as they, without all shame, ~~And (to conclude)~~ ^{And (to conclude)} most of all, let them be ashamed of Man, and afraide of the dreadfull and Iuste Iudge: both Folishly or Maliciously to deuise: and then, deuilishly to father their new fond Monsters on me: Innocent, in hand and hart: for trespassing either against the lawe of God, or Man, in any my Studies or Exercises, Philosophicall, or Mathematicall: As in due time, I hope, will be more manifest.

NOW end I, with **Archemastrie**. Which name, is not so new, as this Arte is rare. For an other Arte, vnder this, a degree (for skill and power) hath bene indued with this English name before. And yet, this, may serue for our purpose, sufficiently, at this present. This Arte, teacheth to bryng to actuall experience sensible,

all worthy conclusions by all the Artes Mathematicall
 purposed, & by true Naturall Philosophie concluded: &
 both addeth to them a farder scope, in the termes of the
 same Artes, & also by hys propre Method, and in peculier
 termes, procedeth, with helpe of the foresayd Artes, to the
 performance of complet Experiēces, which of no particular
 Art, are hable (Formally) to be challenged. If you remember,
 how we considered *Architecture*, in respect of all common
 handworkes: some light may you haue, therby, to vnderstand the
 Souerainty and propertie of this Science. *Science* I may call it,
 rather, then an Arte: for the excellency and Mastershypp it hath,
 ouer so many, and so mighty Artes and Sciences. And bycause it
 procedeth by *Experiences*, and searcheth forth the causes of
 Conclusions, by *Experiences*: and also putteth the Conclusions
 them selues, in *Experience*, it is named of some, *Scientia*
Experimentalis. The *Experimentall Science*. *Nicolaus Cusanus*
 termeth it so, in hys *Experimentes Statikall*, And an other
~~Philosophy~~ *Philosophy* and *Nature* (the floure of whose worthy fame, can
 neuer dye nor wither) did write therof largely, at the request of
Clement the sixt. The Arte carrieth with it, a wonderfull Credit: By
 reason, it certifieth, sensibly, fully, and completely to the vtmost
 power of Nature, and Arte. This Arte, certifieth by *Experience*
 complete and absolute: and other Artes, with their Argumentes,
 and Demonstrations, persuade: and in wordes, proue very well
 their Conclusions.* ~~But~~ wordes, and Argumentes, are no sensible
 certifying: nor the full and finall frute of Sciences practisable. And
 though some Artes, haue in them, *Experiences*, yet they are not
 complete, and brought to the vttermost, they may be stretched
 vnto, and applyed sensibly. As for example: the Naturall
 Philosopher disputeth and maketh goodly shew of reason: And the
 Astronomer, and the Opticall Mechanicien, put some thynges in
Experience: but neither, all, that they may: nor yet sufficiently, and
 to the vtmost, those, which they do, There, then, the *Archemaster*
 steppeth in, and leadeth forth on, the *Experiences*, by order of his
 doctrine *Experimentall*, to the chief and finall power of Naturall

and Mathematicall Artes. Of two or three men, in whom, this Description of *Archemastery* was *Experimentally*, verified, I haue read and hard: and good record, is of their such perfection. So that, this Art, is no fantastick Imagination: as some Sophister, might, *Cum suis Insolubilibus*, make a flourish: and dassell your Imagination: and dash your honest desire and Courage, from beleuing these thinges, so vnheard of, so meruaylous, & of such Importance. Well: as you will. I haue forewarned you. I haue done the part of a frende: I haue discharged my Duety toward God: for my small Talent, at hys most mercyfull handes receiued. To this Science, doth the *Science Alnirangiat*, great Seruice. Muse nothyng of this name. I chaunge not the name, so vsed, and in Print published by other: beyng a name, propre to the Science. Vnder this, commeth *Ars Sintrillia*, by *Artephius*, briefly written. But the chief Science, of the Archemaster, (in this world) as yet knowen, is an other (as it were) OPTICAL Science: wherof, the name shall be told (God willyng) when I shall haue some, (more iust) occasion, therof, to Discourse.

Here, I must end, thus abruptly (Gentle frende, and vnfayned louer of honest and necessary verities.) For, they, who haue (for your sake, and vertues cause) requested me, (an old forworne Mathematicien) to take pen in hand: (through the confidence they reposed in my long experience: and tryed sincerity) for the declaryng and reportyng somewhat, of the frute and commodity, by the Artes Mathematicall, to be atteyned vnto: euen they, Sore agaynst their willes, are forced, for sundry causes, to satisfie the workemans request, in endyng forthwith: He, so feareth this, so new an attempt, & so costly: And in matter so slenderly (hetherto) among the common Sorte of Studentes, considered or esteemed.

And where I was willed, somewhat to alledge, why, in our vulgare Speche, this part of the Principall Science of *Geometrie*, called *Euclides Geometricall Elementes*, is published, to your handlyng: being vnlatined people, and not Vniuersitie Scholers: Verily, I thinke it nedelesse.

mour, and Estimation of the Vniuersities, and Graduates, is,
hereby, nothing diminished. Seing, from, and by their Nurse
Children, you receaue all this Benefite: how great soeuer it be.

: their Studies, hereby, any whit hindred. No more, then the Italian
Vniuersities, as *Academia Bononiensis*, *Ferrariensis*, *Florentina*,
Mediolanensis, *Patauina*, *Papiensis*, *Perusina*, *Pisana*, *Romana*,
Senensis, or any one of them, finde them selues, any deale,
disgraced, or their Studies any thing hindred, by *Frater Lucas de*
Burgo, or by *Nicolaus Tartalea*, who in vulgar Italian language,
haue published, not onely *Euclides Geometrie*, but of *Archimedes*
somewhat: and in Arithmetike and Practicall Geometrie, very large
volumes, all in their vulgar speche. Nor in Germany haue the
famous *Vniuersities*, any thing bene discontent with *Albertus*
Durerus, his Geometricall Institutions in Dutch: or with *Gulielmus*
Xylander, his learned translation of the first sixe bookes of
Euclide, out of the Greke into the high Dutch. Nor with *Gualterus*
H. Riffius, his Geometricall Volume: very diligently translated into
the high Dutch tounge, and published. Nor yet the *Vniuersities* of
Spaine, or Portugall, thinke their reputation to be decayed: or
suppose any their Studies to be hindred by the Excellent
P. Nonnius, his Mathematicall workes, in vulgare speche by him
put forth. Haue you not, likewise, in the French tounge, the whole
Mathematicall Quadriuie? and yet neither Paris, Orleance, or any
of the other Vniuersities of Fraunce, at any time, with the
Translators, or Publishers offended: or any mans Studie thereby
hindred?

, the Common and Vulgar Scholer (much more, the Gramarian)
before his comming to the *Vniuersitie*, shall (or may) be, now
(according to *Plato* his Counsell) sufficiently instructed in
Arithmetike and *Geometrie*, for the better and easier learning of all
maner of *Philosophie*, *Academicall*, or *Peripateticall*. And by that
meanes, goe more cherefully, more skilfully, and spedily forward,
in his Studies, there to be learned. And, so, in lesse time, profite
more, then (otherwise) he should, or could do.

good and pregnant Englishe wittes, of young Gentlemen, and of other, who neuer intend to meddle with the profound search and Studie of Philosophie (in the *Vniuersities* to be learned) may neuerthesse, now, with more ease and libertie, haue good occasion, vertuously to occupie the sharpnesse of their wittes: where, els (perchance) otherwise, they would in fond exercises, spend (or rather leese) their time: neither seruing God: nor furduring the Weale, common or priuate.

Comfort, with good hope, may the *Vniuersities* haue, by reason of this *Englishe* Geometrie, and Mathematicall Præface, that they (hereafter) shall be the more regarded, esteemed, and resorted vnto. For, when it shall be knowne and reported, that of the *Mathematicall Sciences* onely, such great Commodities are ensuing (as I haue specified): and that in dede, some of you vnlatined Studentes, can be good witnesse, of such rare fruite by you enioyed (thereby): as either, before this, was not heard of: or els, not so fully credited: Well, may all men coniecture, that farre greater ayde, and better furniture, to winne to the Perfection of all Philosophie, may ~~in the~~ *Vniuersities* be had: being the Storehouses & Threasury of all Sciences, and all Artes, necessary for the best, and most noble State of Common Wealthes’.

s, how many a Common Artificer, is there, in these Realmes of England and Ireland, that dealeth with Numbers, Rule, & Cumpasse: Who, with their owne Skill and experience, already had, will be hable (by these good helpes and informations) to finde out, and deuise, new workes, straunge Engines, and Instrumentes: for sundry purposes in the Common Wealth? or for priuate pleasure? and for the better maintayning of their owne estate? I will not (therefore) fight against myne owne shadowe. For, no man (I am sure) will open his mouth against this Enterprise. No mã (I say) who either hath Charitie toward his brother (and would be glad of his furtherance in vertuous knowledge): or that hath any care & zeale for the bettering of the Cõmon state of this Realme. Neither any, that make accompt, what the wiser sort of men (Sage

and Stayed) do thinke of them. To none (therefore) will I make any *Apologie*, for a vertuous acte doing: and for cōmending, or setting forth, Profitable Artes to English men, in the English tounge. But, vnto God our Creator, let vs all be thankefull: for that, *As he, of his Goodnes, by his Powre, and in his wisdom hath Created all thynges, in Number, Waight, and Measure:* So, to vs, of hys great Mercy, he hath reuealed Meanes, whereby, to attayne the sufficient and necessary knowledge of the foresayd hys three principall Instrumentes: Which Meanes, I haue abundantly proued vnto you, to be the *Sciences and Artes Mathematicall*.

And though I haue ben pinched with straightnes of tyme: that, no way, I could so pen downe the matter (in my Mynde) as I determined: hoppyng of conuenient laysure: Yet. if vertuous zeale, and honest Intent prouoke and bryng you to the readyng and examinyng of this Compendious treatise, I do not doute, but, as the veritie therof (accordyng to our purpose) will be euident vnto you: So the pith and force therof, will perswade you: and the wonderfull frute therof, highly pleasure you. And that you may the easier perceiue, and better remember, the principall pointes, whereof my Preface treateth, *The Ground platt of this Preface* ~~and give you~~ the Groundplatt of my whole discourse, in a Table annexed: from the first to the last, somewhat Methodically contriued.

If Hast, hath caused my poore pen, any where, to stumble: You will, (I am sure) in part of recompence, (for my earnest and sincere good will to pleasure you), Consider the rockish huge mountaines, and the perilous vnbeaten wayes, which (both night and day, for the while) it hath toyled and labored through, to bryng you this good Newes, and Comfortable profe, of Vertues frute.

So, I Commit you vnto Gods Mercyfull direction, for the rest:
hartely

besechyng hym, to prosper your Studyes, and honest Intentēs:
to his Glory, & the Commodity of our Countrey. *Amen.*

*Written at my poore House
At Mortlake.*

Anno. 1570. February. 9.

J. DEE

Here haue you (according to my promisse) the Groundplat of
my MATHEMATICALL Præface: annexed to *Euclide* (now first)
published in our Englishe tounge. An. 1570. Febr. 3.

Principall, which are two, onely,	Arithmetike.	<i>Simple, Which dealeth with Numbers onely: and demonstrateth all their properties and appertenances: where, an Vnit, is Indiuisable.</i>	The vse whereof, is either,	<i>In thinges Supernaturall, æternall, & Diuine: By Application, Ascending.</i>	The like Vses and Appli- cations are, (though in a degree lower) in the Artes Mathematicall Deriuatiue.
	Geometrie.	<i>Mixt, Which with aide of Geometrie principall, demonstrateth some Arithmeticall Conclusion, or Purpose.</i> <i>Simple, Which dealeth with Magnitudes, onely: and demonstrateth all their properties, passions, and appertenances: whose Point, is Indiuisable.</i> <i>Mixt, Which with aide of Arithmetike principall, demonstrateth some Geometricall purpose, as EVCLIDES ELEMENTES.</i>		<i>In thinges Mathematicall: without farther Application.</i> <i>In thinges Naturall: both Substãtiãll, & Accidentall, Visible, & Inuisible. &c. By Application: Descending.</i>	
Sciences, and Artes Mathe- maticall, are, either		Arithmetike, <i>vulgar: which consi- dereth</i>		Arithmetike of most vsuall whole numbers: And of Fractions to them appertaining. Arithmetike of Proportions. Arithmetike Circular. Arithmetike of Radicall Nübers: Simple, Compound, Mixt: And of their Fractions. Arithmetike of Cossike Nübers: with their Fractions: And the great Arte of Algiebar.	
	The names of the Princi- palls: as,		At hand	All Lengthes.— All Plaines: As, Land, Borde, Glasse, &c. All Solids: As, Timber, Stone, Vessels, &c.	Mecometrie. Embadometrie. Stereometrie.
		Geometrie, vulgar: <i>which teacheth Measuring</i>		How farre, from the Measurer, any thing is: of him sene, on Land or Water: called Apomecometrie.	Geodesie: more cunningly to Measure and Survey Landes, Woods, Waters. &c.
Deriuatiue frõ the Princi- palls: of which, some haue			With distãce from the thing Measured, as,	How high or deepe, from the leuell of the Measurers standing, any thing is: Seene of hym, on Land or Water: called Hypsometrie.	Of which are growen the Feates & Artes of
				How broad, a thing is, which is in the Measurers view: so it be situated on Land or Water: called Platometrie.	Stratarithmetrie.
	Perspectiue,			Which demonstrateth the maners and properties of all Radiations: Directe, Broken, and Reflected.	
	Astronomie,			Which demonstrateth the Distances, Magnitudes, and all Naturall motions, Apparences, and Passions, proper to the Planets and fixed Starres: for any time, past, present, and to come: in respecte of a certaine Horizon, or without respecte of any Horizon.	
	Musike,			Which demonstrateth by reason, and teacheth by sense, perfectly to iudge and order the diuersitie of Soundes, hie or low.	
	Cosmographie,			Which, wholly and perfectly maketh description of the Heauenlym and also Elementall part of the World: and of these partes, maketh homologall application, and mutuall collation necessary.	
	Astrologie,			Which reasonably demonstrateth the operations and effectes of the naturall beames of light, and secrete Influence of the Planets, and fixed Starres, in euery Element and Elementall body: at all times, in any Horizon assigned.	
	Statike,			Which demonstrateth the causes of heauines and lightnes of all thinges: and of the motions and properties to heauines and lightnes belonging.	
	Anthropographie,			Which describeth the Nüber, Measure, Waight, Figure, Situation, and colour of euery diuers thing contained in the perfecte body of MAN: and geueth certaine knowledge of the Figure, Symmetrie, Waight, Characterization, & due Locall motion of any percell of the said body assigned: and of numbers to the said percell appertaining.	

*Propre
names
as,*

Trochilike,
Helicosophie,
Pneumatithmie,

Menadrie,

Hypogeiodie,

Hydragogie,

Horometrie,
Zographie,

Architecture,
Nauigation,

Thaumaturgike,
Archemastrie,

Which demonstrateth the properties of all Circular motions: Simple and Compound.
Which demonstrateth the designing of all Spirall lines: in Plaine, on Cylinder, Cone, Sphere, Conoid, and Sphaeroid: and their properties.
Which demonstrateth by close hollow Geometricall figures (Regular and Irregular) the straunge properties (in motion or stay) of the Water, Ayre, Smoke, and Fire, in their Continuities, and as they are ioyned to the Elements next them.
Which demonstrateth, how, aboue Natures Vertue, and power simple: Vertue and force, may be multiplied: and so to directe, to lift, to pull to, and to put or cast fro, any multiplied, or simple determined Vertue, Waight, or Force: naturally, not, so, directible, or moueable.
Which demonstrateth, how, vnder the Sphaericall Superficies of the Earth, at any depth, to any perpendicular line assigned (whose distance from the perpendicular of the entrance: and the Azimuth likewise, in respect of the sayd entrance, is knowne) certaine way, may be prescribed and gone, &c.
Which demonstrateth the possible leading of water by Natures law, and by artificiall helpe, from any head (being Spring, standing, or running water) to any other place assigned.
Which demonstrateth, how, at all times appointed, the precise, vsuall denomination of time, may be knowne, for any place assigned.
Which demonstrateth and teacheth, how, the Intersection of all visuall Pyramids, made by any plaine assigned (the Center, distance, and lightes being determined) may be, by lines, and proper colours represented.
Which is a Science garnished with many doctrines, and diuers Instructions: by whose iudgement, all workes by other workmen finished, are iudged.
Which demonstrateth, how, by the Shortest good way, by the aptest direction, and in the shortest time: a sufficient Shippe, betwene any two places (in passage nauigable) assigned, may be conducted: and in all stormes and naturall disturbances chauncing, how to vse the best possible meanes, to recouer the place first assigned.
Which geueth certaine order to make straunge workes, of the sense to be perceiued: and of men greatly to be wondred at.
Which teacheth to bring to actuall experience sensible, all worthy conclusions, by all the Artes Mathematicall purposed: and by true Naturall philosophie, concluded: And both addeth to them a farder Scope, in the termes of the same Artes: and also, by his proper Method, and in peculiar termes, procedeth, with helpe of the forsayd Artes, to the performance of complete Experiences: which, of no particular Arte, are hable (Formally) to be challenged.

Title Page Text

full text below

THE ELEMENTS
OF GEOMETRIE
of the most auncient
Philosopher
EVCLIDE
of Megara.

*Faithfully (now first) translated
into the Englishe toung, by
H. Billingsley, Citizen of London.
Whereunto are annexed certaine
Scholies, Annotations, and Inuentions,*

of the best Mathematiciens,
both of time past, and
in this our age.

*With a very fruitfull Præface made by M. I. Dee,
specifying the chiefe Mathematicall Sciēces, what
they are, and wherunto commodious: where, also, are disclosed certaine new Secrets Mathematicall
and Mechanicall, vntill these our daies, greatly missed.*

Imprinted at London by *Iohn Daye*.

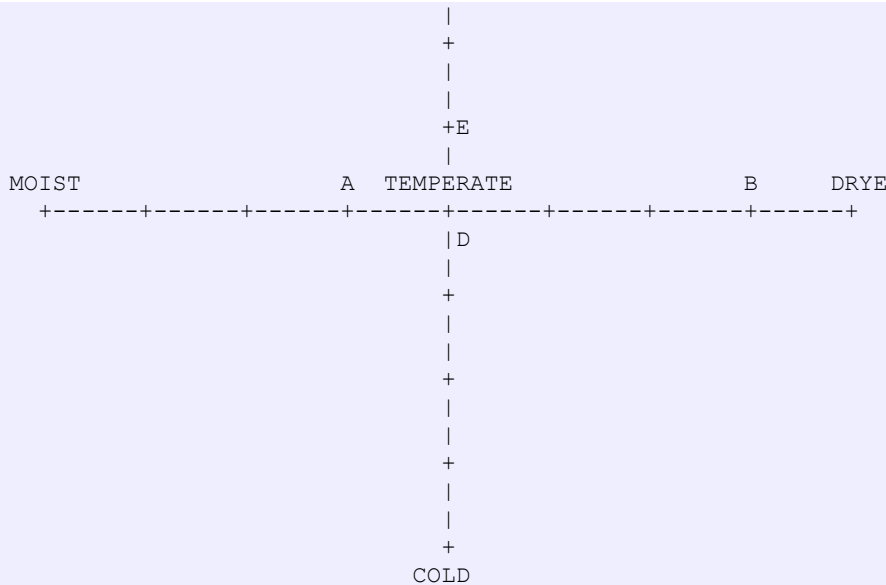
Transcriber's Footnotes

A. Mathematical Notation. John Dee used the “root” sign $\sqrt{}$ in combination with some less familiar symbols:

‘power of 1’ symbol	“First power”, here used to express an unknown. <i>Shown in this e-text as X (capitalized).</i>
square root	Root sign combined with “second power” symbol = square root. <i>Shown in this e-text as $\sqrt[2]{}$.</i>
cube root	Root sign combined with “third power” symbol = cube root. <i>Shown in this e-text as $\sqrt[3]{}$.</i>
cube root	Doubled “second power” symbol = 4th power; with root sign = fourth root. <i>Shown in this e-text as $\sqrt[4]{}$.</i>

B. Diagrams: The symbol drawn as *P* (Pounds) is shown here as *P*. See above for **X** symbol.

HOTE
+C
|
|
+
|



{P}. 2.	Hote. 4.
{P}. 1.	Hote. 3.

{P}. 2.	Hote. 4.	$-\frac{1}{3}$	The forme
{P}. 1.	Hote. 3.	$-\frac{2}{3}$	3 $\frac{2}{3}$ resulting.

C. “Vergilius teaches in his Georgikes.” The quoted lines, with breaks at each “&c.”, are 438-439; 451-457; 463-464.

Euclid citations

The following Propositions were identified by number.

6.12: (How) to find a fourth (line) proportional to three given straight lines.

11.34: In equal parallelepipedal solids the bases are reciprocally proportional to the heights; and those parallelepipedal solids in which the bases are reciprocally proportional to the heights are equal.

11.36: If three straight lines are proportional, then the parallelepipedal solid formed out of the three equals the parallelepipedal solid on the mean which is equilateral, but equiangular with the aforesaid solid.

12.1: Similar polygons inscribed in circles are to one another as the squares on their diameters.

12.2: Circles are to one another as the squares on their diameters.

12.18 (“last”): Spheres are to one another in triplicate ratio of their respective diameters.

Notes on the text

The Greek letter η (eta) was consistently printed as if it were the ou-ligature 8.

The Latin *-que* was written as an abbreviation resembling **-q̇**; . It is shown here as q^{ue}.

Less common words include “fatch” (probably used as a variant of “fetch”) and the mathematical terms “sexagene” and “sexagesme”.

*** END OF THE PROJECT GUTENBERG EBOOK THE
MATHEMATICALL PRAEFACE TO ELEMENTS OF GEOMETRIE OF
EUCLID OF MEGARA ***

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